

**A**  
**MAJOR PROJECT REPORT ON**  
**AN 8-BIT RIPPLE CARRY ADDER USING QUANTUM DOT**  
**CELLULAR AUTOMATA FOR NANOCOMPUTING APPLICATIONS**

**Submitted in partial fulfillment of the requirement for the award of degree of**

**BACHELOR OF TECHNOLOGY**  
**IN**  
**ELECTRONICS AND COMMUNICATION ENGINEERING**

**SUBMITTED BY**

<b>S.AASHRITHA</b>	<b>218R1A04C9</b>
<b>A.SHIVANI</b>	<b>218R1A04D0</b>
<b>A.LAXMI PRIYA</b>	<b>218R1A04D1</b>
<b>A.ARUN</b>	<b>218R1A04D2</b>

**Under the Esteemed Guidance of**

**MR. VASEEM AHMED QURESHI**  
**Associate Professor.**



**DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING**

**CMR ENGINEERING COLLEGE**  
**UGC AUTONOMOUS**

**(Approved by AICTE, Affiliated to JNTU Hyderabad, Accredited by NBA)**  
**Kandlakoya(V), Medchal(M), Telangana – 501401**

**(2024-2025)**

# CMR ENGINEERING COLLEGE

## UGC AUTONOMOUS

(Approved by AICTE, Affiliated to JNTU Hyderabad, Accredited by  
NBA) Kandlakoya (V), Medchal Road, Hyderabad - 501 401

### DEPARTMENT OF ELECTRONICS AND COMMUNICATION ENGINEERING



### CERTIFICATE

This is to certify that Major project work entitled “AN 8-BIT RIPPLE CARRY ADDER USING QUANTUM DOT CELLULAR AUTOMATA FOR NANO COMPUTING APPLICATIONS” is being submitted by S.AASHRITHA bearing Roll No: 218R1A04C9, A.SHIVANI bearing Roll No: 218R1A04D0, A.LAXMI PRIYA bearing Roll No: 218R1A04D1, A.ARUN bearing Roll No: 218R1A04D2 in B.Tech IV-II semester, Electronics and Communication Engineering is a record bonafide work carried out by them during the academic year 2024-25. The results embodied in this report have not been submitted to any other University for the award of any degree

INTERNAL GUIDE

**MR. VASEEM AHMED QURESHI**

**Associate Professor**

HEAD OF THE DEPARTMENT

**Dr. SUMAN MISHRA**

**Professor**

**EXTERNAL EXAMINER**

## ACKNOWLEDGEMENTS

We sincerely thank the management of our college **CMR Engineering College** for providing the required facilities during our project work. We derive great pleasure in expressing our sincere gratitude to our Principal **Dr. A. S. Reddy** for his timely suggestions, which helped us to complete the project work successfully. It is the very auspicious moment we would like to express our gratitude to **Dr. SUMAN MISHRA**, Head of the Department, ECE for his consistent encouragement during the progress of this project.

We take it as a privilege to thank our major project coordinator **Dr. T. SATYANARAYANA**, Associate Professor, Department of ECE for the ideas that led to complete the project work and we also thank him for his continuous guidance, support and unfailing patience, throughout the course of this work. We sincerely thank our project internal guide **Mr.VASEEM AHMED QURESHI**, Associate Professor of ECE for guidance and encouragement in carrying out this project work.

## **DECLARATION**

We hereby declare that the Major project entitled “**AN 8-BIT RIPPLE CARRY ADDER USING QUANTUM DOT CELLULAR AUTOMATA FOR NANO COMPUTING APPLICATIONS**” is the work done by us in campus at **CMR ENGINEERING COLLEGE**, Kandlakoya during the academic year 2024-2025 and is submitted as major project in partial fulfillment of the requirements for the award of degree of **BACHELOR OF TECHNOLOGY in ELECTRONICS AND COMMUNICATION ENGINEERING FROM JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY, HYDERABAD.**

<b>S.AASHRITHA</b>	<b>(218R1A04C9)</b>
<b>A.SHIVANI</b>	<b>(218R1A04D0)</b>
<b>A.LAXMI PRIYA</b>	<b>(218R1A04D1)</b>
<b>A.ARUN</b>	<b>(218R1A04D2)</b>

# ABSTRACT

Quantum-dot Cellular Automata (QCA) technology represents a significant advancement over traditional CMOS technology, offering benefits such as reduced power consumption, higher clock speeds, and increased circuit density. This technology utilizes quantum dots to encode binary information and holds promise for overcoming many of CMOS's physical limitations, making it a promising candidate for future Very-Large-Scale Integration (VLSI) circuits.

In this study, we introduce a high-performance 8-bit Ripple Carry Adder (RCA) designed using QCA technology. The RCA comprises a series of interconnected Full-adders, each constructed with QCA cells arranged to execute binary addition efficiently. This design focuses on optimizing carry propagation and reducing overall cell counts, which improves the performance metrics of the adder circuit for nano computing arithmetic circuits.

The proposed method involves leveraging our QCA-based 8-bit Ripple Carry Adder, which will have significant implications for future VLSI circuits. This approach will enhance performance and density, making it ideal for high-speed arithmetic circuits. Additionally, the method will provide substantial power savings, emphasizing its potential for energy-efficient computing. The optimized design will also allow for scalability, accommodating more complex circuits and supporting larger bit-width adders as well as advanced electronic systems. Overall, this QCA technology is poised to surpass the limitations of CMOS and drive the advancement of next-generation electronic devices.

# CONTENTS

	Page No.
CERTIFICATE	I
DECLARATION BY THE CANDIDATE	II
ACKNOWLEDGEMENT	III
ABSTRACT	IV
CONTENTS	V
LIST OF FIGURES	VII
LIST OF TABLES	IX
<b>CHAPTER-1</b>	
<b>1. INTRODUCTION</b>	<b>1</b>
1.1 OVERVIEW OF THE PROJECT	2
1.2 OBJECTIVE OF THE PROJECT	3
1.3 ORGANIZATION OF THE PROJECT	4
<b>CHAPTER-2</b>	
<b>2. LITERATURE SURVEY</b>	<b>7</b>
<b>CHAPTER-3</b>	
<b>3. SOFTWARE REQUIREMENTS</b>	<b>12</b>
3.1 QCA DESIGNER	12
3.1.1 Key features of qca designer 2.0.3	13
3.1.2 Common use cases for qca designer 2.0.3	15
3.1.3 How to download and qca designer 2.0.3	15
<b>CHAPTER-4</b>	
<b>4. QCA FUNDAMENTALS</b>	<b>18</b>
4.1 QCA BASICS	18
4.2 QCA CELL	19
4.3 QCA IMPLEMENTATION TECHNIQUES	24
4.3.1 Metal island	25
4.3.2 Semiconductor	25
4.3.3 Molecular qca	26

4.3.4 Magnetic qca	28
4.4 QCA DEVICES	29
4.5 QCA CLOCKING	30
4.6 QCA WIRE CROSSING	32
4.6.1 Kink energy and cell robustness	34
4.7 MODELING QCA DESIGNS	34
4.7.1 QCA power dissipation model	37
4.8 SUMMARY	40
<b>CHAPTER-5</b>	
<b>5. QCA ADDERS</b>	<b>41</b>
5.1 FULL ADDER	41
5.2 2-BIT RCA	42
5.3 4-BIT RCA	43
5.4 8-BIT RCA	45
<b>CHAPTER- 6</b>	
<b>6. RESULTS</b>	<b>47</b>
6.1 SIMULATION RESULTS	47
6.2 ENERGY DISSIPATION OF ADDERS	49
<b>CHAPTER- 7</b>	
<b>7. CONCLUSION AND FUTURE SCOPE</b>	<b>53</b>
7.1 CONCLUSION	53
7.2 APPLICATIONS	54
7.3 ADVANTAGES	56
7.4 FUTURESCOPE	58
<b>REFERENCES</b>	<b>59</b>
<b>APPENDIX</b>	<b>60</b>

# LIST OF FIGURES

		Page No.
Figure 3.1	Flow chart for making an 8-Bit Ripple Carry Adder using Quantum dot cellular automata for nano computing applications	17
Figure 3.2	Two possible polarization of QCA cells	20
Figure 3.3	Various quantized energy states of an electron in a one-dimensional infinite potential well	22
Figure 3.4	Roller coaster example for tunneling phenomenon across a finite potential wall	22
Figure 3.5	Clock energy variation to control the tunneling barrier	23
Figure 3.6	Sem image of metal-QCA cell and corresponding schematics diagrams	26
Figure 3.7	(a) silicon-based QCA schematics and sem images (b) electron micrograph of a gaas/algaas QCA cell with simplified circuit equivalent of the 4-dot cell	27
Figure 3.8	Two views of molecule as a QCA cell	28
Figure 3.9	Different possible states of molecule a show a +1state, b show a non-ideal state that is a unwanted state, and c show a 1state	29
Figure 3.10	Sem image of a room temperature mq ca network	30
Figure 3.11	Implementation of majority gate for magnetic Quantum-dot cellular automata	30
Figure 3.12	QCA Premtives: (a) 2 Different realizations of inverter (b) Original majority gate and rotated majority gate (c) QCA Wire	32
Figure 3.13	QCA Clocking with 4 phases	32
Figure 3.14	Wire crossing (a) Multi Layer (b) Coplanar	33

Figure 3.15	Wire crossing using clock zone (a)Cells on the switch phase cross cells on the release phase (b)Cells on the hold phase cross cells on the relax phase	34
Figure 3.16	I/O and clocking signals for clock zonebased crossover	34
Figure 3.17	Power flows between 2 qca cells	39
Figure 5.1	Full adder layout using QCA Designer 2.0.3	43
Figure 5.2	2-Bit RCA layout using QCA Designer 2.0.3	44
Figure 5.3	4-Bit RCA layout using QCA Designer 2.0.3	45
Figure 5.4	8-Bit RCA layout using QCA Designer 2.0.3	47
Figure 6.1.1	Full adder simulations using QCA Designer 2.0.3	48
Figure 6.1.2	2-Bit RCA simulations using QCA Designer 2.0.3	48
Figure 6.1.3	4-Bit RCA simulations using QCA Designer 2.0.3	49
Figure 6.1.4	8-Bit RCA simulations using QCA Designer 2.0.3	49
Figure 6.2.1	Energy analysis of full adder using QCA Designer E	50
Figure 6.2.2	Energy analysis of 2-Bit RCA using QCA Designer E	50
Figure 6.2.3	Energy analysis of 4-BIT RCA using QCA Designer E	51
Figure 6.2.4	Energy analysis of 8-BIT RCA using QCA Designer E	51

## LIST OF TABLES

		<b>Page No.</b>
Table 3.1	Bistable approximation and coherence vector parameters model	36
Table 6.1	Comparision of Energy Dissipation	53

# CHAPTER 1

## INTRODUCTION

The Complementary Metal-Oxide-Semiconductor (CMOS) technology is used to develop digital logic circuits. But this technology has recently faced challenges and drawbacks such as high temperature, leakage current, and ultra-low power. Therefore, numerous studies have been done to identify a good substitute for this technology. Quantum-dot Cellular Automata (QCA) technology is introduced as a new technique at nanoscale to replace the CMOS technology.

-This technology offers several advantages over traditional CMOS for VLSI circuits. It provides higher integration densities, lower power consumption, and potentially faster processing speeds due to the utilization of quantum properties. These advancements make QCA a promising solution to address the inherent limitations of CMOS technology. They use quantum effects rather than electric current to perform operations in this technology. The core element of this technology is the QCA cell. Each cell has a square structure that includes four dots in its corners.

Two electrons move freely between these dots. Due of the electrostatic repulsion between these electrons, electrons tend to reside in diameter square. Many different structures have been suggested to carry out addition operations, and has advantages and disadvantages in comparison to other designs. This paper has two new ideas. The first idea is to design a Full-adder in QCA technology. The second idea is to design a 8-bit RCA using the presented Full-adder in QCA technology. The core element of this technology is the QCA cell. Each cell has a square structure that includes four dots in its corners. The second idea is to design a 8-bit RCA using the presented Full-adder in QCA technology.

The QCADesigner 2.0.3 tool is utilized to simulate these two designs. The result of simulation demonstrates that the presented structure outperforms all earlier designs based on latency, cell counts, and occupied area. The main contributions of the suggested RCA and Full-adder circuits are:

- Reducing the number of cells compared to previous designs
- Decreasing the occupied area compared to previous designs
- Decreasing the complexity circuit compared to previous designs
- Calculating the power dissipation of the suggested Full-adder layout

## 1.1 OVERVIEW OF THE PROJECT

The rapid miniaturization of electronic components has led to growing concerns about the performance and energy efficiency of traditional CMOS-based devices. In response to these challenges, Quantum Dot Cellular Automata (QCA) has emerged as a promising alternative for nano-scale computing. QCA operates using quantum dots arranged in cells, where information is encoded in the configuration of these dots, allowing for ultra-low-power and high-speed computation. This project aims to design and implement an 8-bit Ripple Carry Adder (RCA) using QCA technology, exploring its viability for future nano-computing applications. The adder, a fundamental building block in digital systems, will serve as a test case for evaluating the potential of QCA in performing basic arithmetic operations efficiently at the nanoscale.

The project is expected to result in several key outcomes. First, it will demonstrate the design and functionality of an 8-bit Ripple Carry Adder using QCA. Second, it will provide a detailed performance comparison with traditional CMOS-based adders, particularly in terms of power consumption, speed, and area efficiency. These findings will contribute valuable insights into the potential of QCA for digital computation, shedding light on its ability to address the limitations of CMOS technology.

Furthermore, the project will explore the scalability of QCA for larger adder designs and more complex computational circuits, paving the way for the development of future QCA-based nano-computing systems. This project aims to design and implement an 8-bit Ripple Carry Adder (RCA) using QCA technology, exploring its viability for future nano-computing applications.

In conclusion, this project represents an exciting step towards realizing the potential of Quantum Dot Cellular Automata for next-generation nano-computing applications. By implementing an 8-bit Ripple Carry Adder using QCA, the research will advance our understanding of QCA technology and its capabilities in constructing efficient, low-power, and high-performance digital circuits.

The insights gained could have profound implications for the design of ultra-low-power, high-performance processors and computational systems in the coming decades, as we move closer to the limits of traditional semiconductor technologies. By implementing an 8-bit Ripple Carry Adder using QCA, the research will advance our understanding of QCA technology.

## 1.2 OBJECTIVE OF THE PROJECT

The primary objective of this project is to design and implement an 8-bit Ripple Carry Adder (RCA) using Quantum Dot Cellular Automata (QCA) technology, with a focus on exploring the potential of QCA for efficient nano-computing applications. The RCA is a fundamental digital circuit that performs binary addition, and by implementing it using QCA, the project aims to demonstrate the feasibility of this emerging nanotechnology for constructing low-power, high-performance arithmetic circuits. This design will serve as a critical step in assessing the capabilities of QCA for practical use in nano-scale computation, a key area of research as conventional CMOS technologies face limitations at smaller process nodes.

Key performance metrics, such as power consumption, circuit area, and propagation delay (speed), will be carefully analyzed. The goal is to demonstrate that QCA can provide significant advantages over traditional CMOS designs, particularly in terms of power efficiency and speed, making it a suitable alternative for future ultra-low-power computing systems at the nanoscale. Another objective is to investigate the scalability of QCA-based designs, particularly how easily an 8-bit RCA can be extended to larger bit-width adders or integrated into more complex arithmetic circuits. This scalability is essential for the potential future use of QCA in building full-fledged processors or computational units that require fast and low-power operations.

Finally, the project aims to provide a comprehensive analysis of the design and simulation process, contributing to the broader understanding of QCA as a viable alternative to conventional digital logic. By achieving these objectives, the project will pave the way for future research into the application of QCA in practical nano-computing systems, offering solutions to challenges faced by current semiconductor technologies and contributing to the evolution of ultra-low-power digital circuits for next-generation computing. Key performance metrics, such as power consumption, circuit area, and propagation delay (speed), will be carefully analyzed.

By achieving these objectives, the project will pave the way for future research into the application of QCA in practical nano-computing systems. Another objective is to investigate the scalability of QCA-based designs. By achieving these objectives, the project will pave the way for future research into the application of QCA in practical nano-computing systems. By achieving these objectives, the project will pave the way for future research into the application of QCA.

## **1.3 ORGANIZATION OF THE PROJECT**

This project will be organized into several key phases, each focused on different aspects of the design, simulation, and evaluation of the 8-bit Ripple Carry Adder (RCA) using Quantum Dot Cellular Automata (QCA) for nano-computing applications. The project is structured to ensure a systematic approach to both the theoretical and practical challenges involved in implementing QCA-based digital circuits.

### **Phase 1: Literature Review and Background Research**

The initial phase will involve an extensive review of existing literature related to Quantum Dot Cellular Automata, Ripple Carry Adders, and nano-computing applications. This phase will provide a deep understanding of the principles behind QCA, its advantages and limitations, and its current status in the context of digital circuit design. It will also explore previous research on implementing basic logic gates and adders using QCA, helping to identify key challenges and solutions. Additionally, this phase will review the performance of conventional CMOS-based adders to establish a baseline for comparison in later phases.

### **Phase 2: Design of Basic QCA Logic Gates**

In the second phase, the project will focus on designing the fundamental logic gates required for the 8-bit Ripple Carry Adder, such as XOR, AND, and OR gates. These gates are the building blocks for the full adder, and their design in QCA will be critical to the success of the overall project. The goal in this phase is to optimize the number of QCA cells needed for each gate while ensuring they perform correctly and efficiently.

### **Phase 3: implementation of Full Adder**

Implementing a **Full Adder** using **Quantum Dot Cellular Automata (QCA)** is a fascinating topic because QCA is an emerging technology for implementing digital logic circuits at the nanoscale. In a quantum dot cellular automata, logic operations are performed based on the arrangement and movement of charge distributions in a lattice of quantum dots. These charge distributions represent binary states (0 or 1). The main challenge lies in efficiently arranging the quantum dot cells to perform these operations at the nanoscale, leveraging QCA's ability to manipulate charge states to represent binary values. In a quantum dot cellular automata, logic operations are performed based on the arrangement and movement of charge distributions in a lattice of quantum dots.

### **Phase 4: Implementation of the 4-Bit Ripple Carry Adder**

Implementing a **4-bit Ripple Carry Adder (RCA)** using **Quantum Dot Cellular Automata (QCA)** involves creating a series of full adders that connect the carry-out of each stage to the carry-in of the next. The QCA technology provides an efficient means to implement these logic gates at a nanoscale level, with each gate constructed using QCA cells. The design involves chaining four full adders, where the carry-out from each stage propagates to the next stage's carry-in.

The final output includes the sum bits and the carry-out bit. This design allows for the efficient implementation of binary addition at a very small scale, leveraging the advantages of QCA's low power consumption and high-speed operation at the nanoscale. However, to implement this practically, you would need to use QCA design tools like **QCADesigner** for simulating and generating the layout of these logic gates and circuits.

### **Phase 5: Implementation of the 8-Bit Ripple Carry Adder**

Once the basic QCA gates are designed and verified, the next phase will focus on using these gates to construct the full 8-bit Ripple Carry Adder. In this phase, the individual full adders will be linked together to form the complete 8-bit RCA. Each full adder will consist of QCA-based XOR, AND, and OR gates. The project will address the challenges associated with carry propagation and ensure that the RCA functions correctly across all bits. This phase will require close attention to detail in order to minimize delays due to carry propagation while maintaining a compact and efficient layout.

### **Phase 6: Simulation and Performance Evaluation**

After implementing the 8-bit RCA, the project will move on to the simulation phase. Using QCA simulation tools, the functionality of the 8-bit adder will be tested to verify its correctness. The performance of the RCA will be evaluated based on key metrics such as power consumption, area efficiency, and propagation delay. This phase will involve running multiple simulations to test the adder under different conditions and input patterns. The results will be compared to traditional CMOS-based adders to assess the advantages and limitations of using QCA in digital circuit design. The performance of the RCA will be evaluated based on key metrics such as power consumption, area efficiency, and propagation delay. This phase will involve running multiple simulations to test the adder under different conditions and input patterns.

### **Phase 7: Optimization and Refinement**

Based on the results from the simulation and performance evaluation phase, the project will enter an optimization phase. In this phase, the design of the RCA and the individual logic gates will be refined to improve performance metrics such as power consumption and speed. This may involve adjusting the number of QCA cells used, minimizing interconnect lengths, or exploring alternative layout configurations. The goal of this phase is to achieve a more efficient design that maximizes the potential benefits of QCA while addressing any performance bottlenecks identified during simulations. In this phase, the design of the RCA and the individual logic gates will be refined to improve performance metrics such as power consumption and speed.

### **Phase 8: Scalability and Extension to Larger Adder Designs**

Once the 8-bit RCA is fully optimized, the next phase will focus on scalability. The project will explore how the QCA-based adder can be extended to larger bit-widths, such as 16-bit or 32-bit adders, by extending the carry propagation chain and assessing the impact on performance. This phase will provide valuable insights into how QCA-based adders can be scaled for use in larger digital systems, such as processors or ALUs, which require more complex arithmetic operations. Additionally, this phase will investigate the potential for integrating the RCA into more complex computational circuits, examining how QCA can be used to build scalable, high-performance processors for future nano-computing applications.

This structured approach ensures that the project covers all critical aspects of QCA-based adder design, from theoretical research to practical implementation and performance evaluation. By dividing the project into clear phases, the research process will be organized, systematic, and focused on achieving the project's objective. The research will provide insights into how QCA can scale up to meet the demands of future nano-computing applications and whether it can be integrated into larger quantum-dot-based systems.

## CHAPTER 2

### LITERATURE SURVEY

1. Pudi, V., Sridharan, K.: ‘Low complexity design of ripple carry and Brent-Kung adders in QCA’, *IEEE Trans. Nanotechnol.*, 2012, **11**, (1), pp. 105–119

The design of adders on quantum dot cellular automata (QCA) has been of recent interest. While few designs exist, investigations on reduction of QCA primitives (majority gates and inverters) for various adders are limited. In this paper, we present a number of new results on majority logic. We use these results to present efficient QCA designs for the ripple carry adder (RCA) and various prefix adders. We derive bounds on the number of majority gates for  $n$ -bit RCA and  $n$ -bit Brent-Kung, Kogge-Stone, Ladner-Fischer, and Han-Carlson adders. We further show that the Brent-Kung adder has lower delay than the best existing adder designs as well as other prefix adders. In addition, signal integrity and robustness studies show that the proposed Brent-Kung adder is fairly well-suited to changes in time-related parameters as well as temperature. Detailed simulations using QCADesigner are presented.

2. M. Vahabi, A. N. Bahar, A. Otsuki and K. A. Wahid, "Ultra-low-cost design of ripple carry adder to design nanoelectronics in QCA nanotechnology," *Electronics*, vol. 11, no. 15, p. 2320, 2022.

Due to the development of integrated circuits and the lack of responsiveness to existing technology, researchers are looking for an alternative technology. Quantum-dot cellular automata (QCA) technology is one of the promising alternatives due to its higher switch speed, lower power dissipation, and higher device density. One of the most important and widely used circuits in digital logic calculations is the full adder (FA) circuit, which actually creates the problem of finding its optimal design and increasing performance. In this project, we designed and implemented two new FA circuits in QCA technology and then implemented ripple carry adder (RCA) circuits. One of the most important and widely used circuits in digital logic calculations is the full adder (FA) circuit.

The proposed FAs and RCAs showed excellent performance in terms of QCA evaluation parameters, especially in cost and cost function, compared to the other

reported designs. The proposed adders' approach was 46.43% more efficient than the best-known design, and the reason for this superiority was due to the coplanar form, without crossovers and inverter gates in the designs.

Many of the RCA designs in QCA technology were implemented with multi-layers but using rotational cells. Furthermore, designing coplanar crossovers with adjacent clock phases in large designs increased latency. For these reasons, we used the minimum crossovers and cells (rotational cells) in our designs. This led to the efficient RCA design of our proposed designs because they were designed as a coplanar (single layer) and with the minimum number of NOT gates, crossovers, and rotational cells.

This made the implemented circuit more stable and robust than previous designs and also significantly superior to previous designs in terms of basic parameters, the number of cells, the occupied area, latency, cost function and cost area-delay. We used the proposed FA in 4-, 8-, 16-, 32-, 64-, and 128-bit ripple carry QCA adder. Due to the comparison and evaluation of the cost function parameter, the cost of implementing the  $n$ -bit RCA of our proposed designs was much lower. The proposed design was 46.43% more efficient in cost function than the best-known design and the reasons for this were due to our innovative and creative design in using the minimum crossovers and inverter gates in the designs. The results showed that the proposed design was more efficient and cost-effective than the existing designs. Therefore, they can be used effectively in the design of more complex circuits and systems and improve and optimize composite and complex circuits

3. S. Seyedi, B. Pourghebleh and N. Jafari Navimipour, "A new coplanar design of a 4-bit ripple carry adder based on quantum-dot cellular automata technology," *ET Circuits, Devices & Systems*, vol. 16, no. 1, pp. 64-70, 2022.

Quantum-dot cellular automata (QCA) is one of the best methods to implement digital circuits at nanoscale. It has excellent potential with high density, fast switching speed, and low energy consumption.

Researchers have emphasized reducing the number of gates, the delay, and the cell count in QCA technology. In addition, a ripple carry adder (RCA) is a circuit in which each full adder's carry-out is the connection for the next full adder's carry-in. These types of adders are quite simple and easily expandable to any desired size. However, they are relatively slow because carries may broadcast across the entire adder. Therefore, an RCA

design on a nanoscale QCA is proposed to diminish the cell number, improve complexity, and decrease latency. The QCADesigner simulation tool is used to verify the correctness of the suggested circuit. The comparison results for the design indicate an approximately 49.14% improvement in cell number and 14.29% advantage in area for the state-of-the-art 4-bit RCA designs with QCA technology. In addition, the obtained results specify the effectiveness of the offered design

QCA is a growing and new technology that has an essential place in nanotechnology and has been studied for several years. Because of the benefits of QCA, namely, high switching speed, low power consumption, and increased device density, it could be an appropriate alternative for CMOS-based circuits. It is also possible to create a logical circuit based on multiple full adders to add  $n$ -bit numbers. In RCA,  $C_{in}$  is connected to the  $C_{out}$  of the previous adder. Because of the RCA's importance in logical circuits, a new coplanar design of a 4-bit RCA to decrease the complexity, energy consumption, number of cells, and area has been proposed in this article. We used both simulation engines of QCADesigner software version 2.0.3 to simulate the recommended designs.

The simulation results using these simulator engines show that the new 4-bit RCA design has an approximately 49.14% advantage in cell number and 14.29% advantage in area over the investigated 4-bit RCA. In addition, the proposed RCA layout contains notably more latency and layer ability than that of previous layouts. The effective structures offered can be used in the future to design  $n$ -bit RCA and high-performance QCA circuits at nanoscale. Consequently, the proposed idea can be a fundamental element in the design of high-speed circuits and other types of adders such as full subtractor and ripple borrow subtractor. In addition, some techniques such as coplanar crossing, multilayer crossing, and logical crossing can be used to connect the outputs or inputs of the proposed designs to other QCA-based circuits.

#### 4. T.N. Sasamal et al. Efficient design of coplanar ripple carry adder in QCA IET Circuits Devices Syst. (2018)

An optimal quantum-dot cellular automata (QCA) design for full adder (FA) based on an optimal three-input exclusive-OR (XOR) gate is presented. This XOR structure utilises a new configuration of cells unlike traditional gate-level approaches. The coplanar QCA FA spans over and delays of 0.5 clock cycles with 40 cells. It achieves total energy dissipation as low as 0.144 eV at 1.5 energy level. The utility of proposed

gate is leveraged to design a ripple-carry adder (RCA) as a specific application. For performance evaluation, the authors use traditional cost metrics and QCA-specific cost function.

Results show that proposed  $n$ -bit RCA outperforms most of the best state-of-the-art designs known in the literature. For example, cell count (area consumption) of 4, 8, and 16 bit adders is 62% (70%), 66% (84%), and 70% (86%) less than the best coplanar RCA design results. In addition, by taking the new cost metrics into account, it is found that proposed adder performs fairly well as compared to the previous adders too. These designs are realised and simulated using QCADesigner.

A new QCA structure-based FA is demonstrated in the work using single layer QCA technology, which can be integrated as a building block for large arithmetic units. We examine the performance of the proposed design and the previous relevant designs via the conventional metrics such as area, delay, complexity, cost of fabrication, and irreversible power dissipation. It is observed that the presented QFA has substantially lower cell counts and area consumption than all previous designs except for multilayer designs, while its latency is less than that of any previous one. We have presented an efficient QCA design for  $n$ -bit RCA where, using the proposed QFA.

It has been shown that the proposed RCA designs have not only offered significantly improvement over all considered coplanar adders but also perform fairly well as compared to the existing multilayer QCA adders and are actually better in most cases. It is observed that the presented QFA has substantially lower cell counts and area consumption than all previous designs except for multilayer designs.

Regarding the QCA-specific cost measurement of, cost of the proposed RCAs are far less than all the previous QCA RCAs including those with alternative carry accelerating techniques. It is also possible to create a logical circuit based on multiple full adders to add  $n$ -bit numbers. In RCA,  $C_{in}$  is connected to the  $C_{out}$  of the previous adder. Because of the RCA's importance in logical circuits, a new coplanar design of a 4-bit RCA to decrease the complexity, energy consumption, number of cells, and area has been proposed in this article.

We used both simulation engines of QCADesigner software version 2.0.3 to simulate the recommended designs. The simulation results using these simulator engines show that the new 4-bit RCA design has an approximately 49.14% advantage in cell number and 14.29% advantage in area over the investigated 4-bit RCA. It is observed that

the presented QFA has substantially lower cell counts and area consumption than all previous designs except for multilayer designs , while its latency is less than that of any previous one.

We examine the performance of the proposed design and the previous relevant designs via the conventional metrics such as area, delay, complexity, cost of fabrication, and irreversible power dissipation. It is observed that the presented QFA has substantially lower cell counts and area consumption than all previous designs except for multilayer designs , while its latency is less than that of any previous one. We have presented an efficient QCA design for  $n$ -bit RCA where , using the proposed QFA.

It has been shown that the proposed RCA designs have not only offered significantly improvement over all considered coplanar adders but also perform fairly well as compared to the existing multilayer QCA adders and are actually better in most cases. It is observed that the presented QFA has substantially lower cell counts and area consumption than all previous designs except for multilayer designs.

## CHAPTER 3

### SOFTWARE REQUIREMENTS

#### 3.1 QCA DESIGNER

QCA Designer 2.0.3 is an advanced software tool specifically developed for the design and simulation of Quantum Dot Cellular Automata (QCA) circuits. This version offers an intuitive user interface, enabling researchers and engineers to easily create, simulate, and analyze QCA structures. With robust features for modeling complex QCA systems, users can visualize the arrangement of quantum dots and their interactions, allowing for comprehensive exploration of various circuit designs.

The software supports the design of a wide range of QCA components, including logic gates, memory elements, and arithmetic circuits, facilitating optimization for performance and energy efficiency. Additionally, QCA Designer 2.0.3 includes import and export functionalities for different design formats, enhancing collaboration and information sharing within the research community. Built-in simulation capabilities allow users to test designs under various conditions, providing critical insights into functionality and reliability. Overall, QCA Designer 2.0.3 is an essential tool for advancing research in QCA technology, contributing significantly to the development of next-generation nanoscale computing systems.

The successful implementation of QCA (Quantum-dot Cellular Automata) realisation of reversible gates using the Layered T Logic Reduction Technique requires a set of specialized software tools and platforms. At the forefront, **QCADesigner** is essential for designing and simulating QCA circuits, providing an intuitive environment to model quantum-dot cellular automata systems with features such as logic gate construction, circuit simulation, and layout visualization. It supports the precise arrangement of cells needed for reversible logic gate implementation.

For the optimization and reduction of logic gates, **MATLAB** or **Python** (with appropriate scientific libraries such as NumPy and SciPy) can be used to perform mathematical computations, data analysis, and logic optimization algorithms, specifically aiding in the T-layered logic reduction technique.

These tools allow the user to automate the complex reduction of logic expressions while evaluating circuit performance metrics such as power dissipation, speed, and area usage. To ensure the accuracy and functionality of the reversible gate

design, a hardware description language (HDL) such as **Verilog** or **VHDL** can be used for simulating the gate-level design, facilitating the verification of logical operations and aiding in the synthesis of the circuits for potential real-world implementations. CAD tools like **Mentor Graphics ModelSim**, **Xilinx Vivado**, or **Cadence** may be employed for simulation and synthesis, enabling further testing of the design in a hardware environment.

Additionally, the system requirements should include a modern **Linux** or **Windows** operating system with sufficient computational resources. A processor with high clock speed, at least 8GB of RAM, and adequate storage are essential to ensure smooth operation of the required software tools and to handle the computationally intensive tasks of QCA circuit simulation and optimization.

QCA Designer 2.0.3 is a specific version of the software tool used for designing and simulating Quantum Dot Cellular Automata (QCA) circuits. QCA is a novel digital technology based on the principles of quantum mechanics, and QCA Designer provides a platform for designing, simulating, and testing QCA-based circuits.

### **3.1.1 Key Features of QCA Designer 2.0.3:**

The core functionality of QCA Designer 2.0.3 is similar to earlier versions, with some improvements in usability, performance, and support for newer QCA-based designs. Here's a more detailed breakdown of its capabilities:

#### **1. QCA Circuit Design:**

- Placement of QCA Cells : Users can place quantum dots (QCA cells) on a grid to form logic gates and interconnecting wires.
- Gate Library : QCA Designer provides a built-in library of basic logic gates such as AND, OR, NOT , and more complex structures like multiplexers, adders, and flip-flops .

#### **2. Simulation :**

- Behavioral Simulation : The software simulates the behavior of QCA circuits, showing how quantum dots respond to clock signals and how information propagates through the circuit.
- Clocking Scheme Simulation : QCA circuits operate under a four-phase

clocking scheme to control the flow of information. QCA Designer 2.0.3 allows you to simulate these phases to ensure proper operation.

- **Energy Consumption and Delay Analysis** : The tool allows for detailed analysis of the power consumption and propagation delay in QCA circuits, helping optimize designs for performance and efficiency.

### **3. Advanced Gate Design :**

- **Custom Gate Design** : Users can design custom logic gates by configuring the arrangement of quantum dots, which can be useful for specialized circuits beyond the basic gates provided in the library.

- **Error Analysis** : QCA is very sensitive to noise and other errors, so the software includes tools for simulating and analyzing the error rates of circuits.

### **4. Circuit Layout :**

- **Layout Editor** : The tool features a layout editor for arranging QCA cells into larger circuit designs. This editor helps visualize the connections between cells and analyze the physical arrangement of the circuit.

- **Wire Design** : Users can create QCA wires, which are made of quantum cells and act as signal transmitters between gates.

### **5. Performance Optimization :**

- **Gate Optimization** : QCA Designer provides mechanisms to improve gate performance, such as reducing the number of cells in a gate or optimizing the layout to minimize delay and power consumption.

- **Compact Circuit Design** : It can help reduce the size of QCA circuits while maintaining or improving their functionality.

### **6. User Interface and Visualization :**

- **Graphical Interface** : QCA Designer 2.0.3 is known for its relatively easy-to-use graphical interface, allowing users to drag and drop cells and wires to construct circuits.

- **Real-Time Simulation** : Users can observe real-time changes in the circuit behavior during simulation, which helps with debugging and verification.

- **Graphical Representation** : The software provides graphical outputs of the

simulation results, including visualizing signal propagation and identifying potential issues with the design.

## **7. Compatibility :**

- Cross-Platform Support : QCA Designer 2.0.3 is typically available for Windows and Linux systems, making it accessible to a wide range of users.
- Export Options : It supports exporting circuit designs to different formats, which may be useful for further analysis or integration with other simulation tools.

### **3.1.2 Common Use Cases for QCA Designer 2.0.3:**

- Designing Digital Logic : Researchers and engineers use QCA Designer to create and simulate QCA-based digital circuits, which can potentially outperform traditional CMOS circuits in terms of speed and power efficiency.
- Nanotechnology Research : As QCA is closely related to nanotechnology, this tool is widely used in research related to nanoscale digital systems.
- Low-Power Computing : With its low energy consumption, QCA is an attractive alternative for building energy-efficient digital systems. QCA Designer 2.0.3 helps evaluate such systems for use in areas like mobile computing, IoT devices, and embedded systems. As QCA is closely related to nanotechnology, this tool is widely used in research related to nanoscale digital systems.
- Quantum Computing : While still in its infancy, QCA is being explored as a potential building block for quantum computing. QCA Designer 2.0.3 can be used to simulate QCA-based components for quantum computing applications.

### **3.1.3 How to Download and Use QCA Designer 2.0.3:**

#### **1. Downloading :**

- QCA Designer 2.0.3 can typically be downloaded from the official QCA Designer website](<http://www.qcadesigner.org/>) or through academic institutions or research groups that provide access to the software.
- Depending on the version, you may need to register or request access, particularly if the software is part of a research initiative.

#### **2. Installation :**

- Windows : The software is usually available as an installer for Windows (e.g.,

` .exe ` format).

- Linux : It might be available as a tarball (`.tar.gz`) or a `.deb` package for installation on Linux distributions.

- Follow the instructions provided in the documentation to install the software on your system.

### **3. Using the Tool :**

- After installation, you can launch the software and start designing QCA circuits by selecting the. New Project option.QCADesigner 2.0.3 is a powerful tool for designing and simulating Quantum-dot Cellular Automata (QCA) circuits

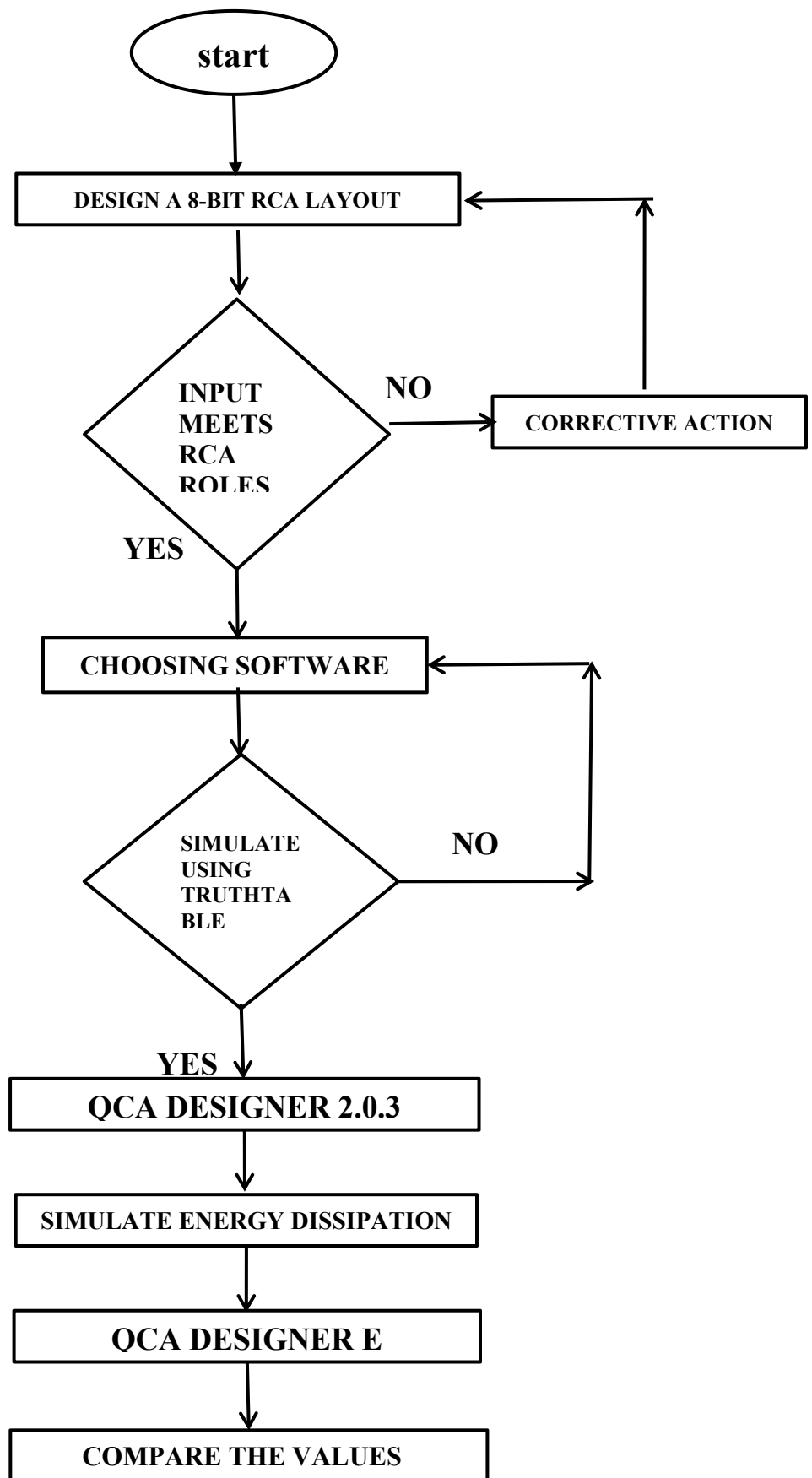
- The interface provides drag-and-drop tools for placing gates and connecting wires. You can also adjust the clocking scheme and run simulations to verify the functionality of your design.

First, download the QCA Designer 2.0.3 software from the official website or a reputable source. Ensure that your computer meets the system requirements, including a compatible operating system, sufficient RAM, and available disk space.

Once the download is complete, run the installer and follow the prompts to install the software. The installation process may take a few minutes, depending on your system's specifications. After the installation is complete, launch the QCA Designer 2.0.3 software.

To get started with QCA Designer 2.0.3, create a new project by selecting "File" > "New Project" from the menu bar. Choose the desired project settings, such as the QCA cell type, grid size, and simulation parameters. After creating the project, you can design and simulate QCA circuits using the software's intuitive interface and tools.

To design a QCA circuit, use the toolbar and menu options to add QCA cells, wires, and other components to the grid. You can also use the software's built-in libraries and templates to speed up the design process. Once you have designed the circuit, you can simulate its behavior using the software's simulation tools and analyze the results.After creating the project, you can design and simulate QCA circuits using the software's intuitive interface and tools.



**Fig3.1** Flow chart for making an 8-bit ripple carry adder using quantum dot cellular automata for nanocomputing applications

## CHAPTER 4

### QCA FUNDAMENTALS

#### 4.1 QCA BASICS

One of the proposed implementations of the Quantum Cellular Automata is the Quantumdot Cellular Automata. Quantum-dot Cellular Automata is not a physical implementation yet, it is rather a lower-level abstraction, since there are several ways to build the quantum dots and connect them. Quantum dots can be any charge containers, with discrete electrical energy states (there may be more than two states, but only two are used), sometimes called artificial atoms. Some molecules have well defined energy states and, therefore, are suitable for supporting the operation of QCA systems.

Small metal pieces can also behave as quantum dots, if the energy states an electron can occupy are distinguishable, instead of the usual energy band. This means that the difference between two consecutive energy states must be well above the thermal noise energy ( $k_B T$ , being  $k_B$  the Boltzmann constant and  $T$  the absolute temperature).

The basic cells are made of four dots placed in the corners of a square, populated with two excess electrons. These dots are well known as quantum dots or q dots. The charge of the electron is localized by the quantum dot. The dot is basically a region of space with energy barriers surrounding it. These barriers are large and high enough so that the charge within it is quantized to a multiple elementary charge. Given the electrostatic interactions (repulsion) between the charges, these will tend to occupy diagonally opposed quantum dots.

There are only two stable configurations, as there are only two diagonals in a square, and these two stable configurations are the two lower energy states referred above: they encode the binary values '0' and '1'. In the absence of any environmental conditions, the two configurations have the same electrostatic energy. The state of the neighboring cells makes one of the configurations to be the preferred low-energy configuration. The bistability of QCA is based on the quantization of charge and it is essential to identify the relationship between the energy levels of a single particle and the energy levels of the dot.

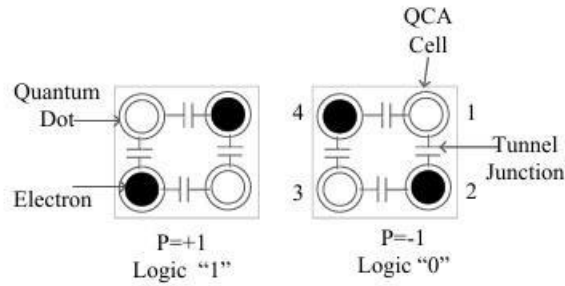
According to the existing Coulombic interaction between the electronic charges, they can occupy diagonal antipodal sites through tunneling junctions. A polarization  $P$  in a cell, which measures the extent to which the electronic charge is distributed among the

four dots, is therefore defined as:

$$p = (p_1 + p_3) - (p_2 + p_4) / p_1 + p_2 + p_3 + p_4 \quad (2.1)$$

Where  $p_i$  is the electronic charge in each dot to favour-dotQCAcell. Once polarized, a QCA cell can be in any one of the two possible states depending on the polarization of charges in the cell. Because of coulombic repulsion, the two most likely polarization states of QCA can be denoted as  $P = +1$  and  $P = -1$  as shown in Fig. 3.2. The two states depicted here are called ‘most likely’ and not the only two polarization states are because of the small (almost negligible) likelihood of existence of an erroneous state.

In QCA architecture, information is transferred between neighboring cells by mutual interaction from cell to cell. Hence, if we change the polarization of the driver cell (left most cell also know as input cell), first its nearest neighbor changes its polarization. Then the next neighbor and so on. Figure 3.2 depicts the transfer of polarization between neighboring QCA cells. When the driver cell (input)



**Fig 4.1: Two possible polarization of qca cells**

is  $P = -1$  (or  $P = +1$ ), a linear transfer of information among its neighboring cells leads to all of them being polarized to  $P = -1$  (or  $P = +1$ ).

## 4.2 QCA Cell

To figure out the operation of a simple QCA cell, we first examine the motion of an electron in an infinite potential well. The walls of infinite potential well hinder electron to tunnel between adjacent dots.

Electrons in an infinite potential well exist as a wave function  $(x, y, z)$  that gives us the probability of finding an electron within that potential well. This probability is proportional to  $|x, y, z|^2$ . Solution to the Schrodinger's wave equation for a free electron ( $V = 0$ ) is given by:

$$d^2\psi/dx^2 + 2m/\hbar^2 (E - V)\psi = 0 \quad (2.2)$$

where  $V$  is the potential acting on the particle,  $E$  is the energy of the particle, and  $m$  is the mass. Taking  $V = 0$  for free electron, we obtain:

$$d^2\psi/dx^2 + 2m/\hbar^2 (E)\psi = 0 \quad (2.3)$$

Using  $k^2 = 2m/\hbar^2 E$ , this reduces to

$$d^2\psi/dx^2 + k^2\psi = 0 \quad (2.4)$$

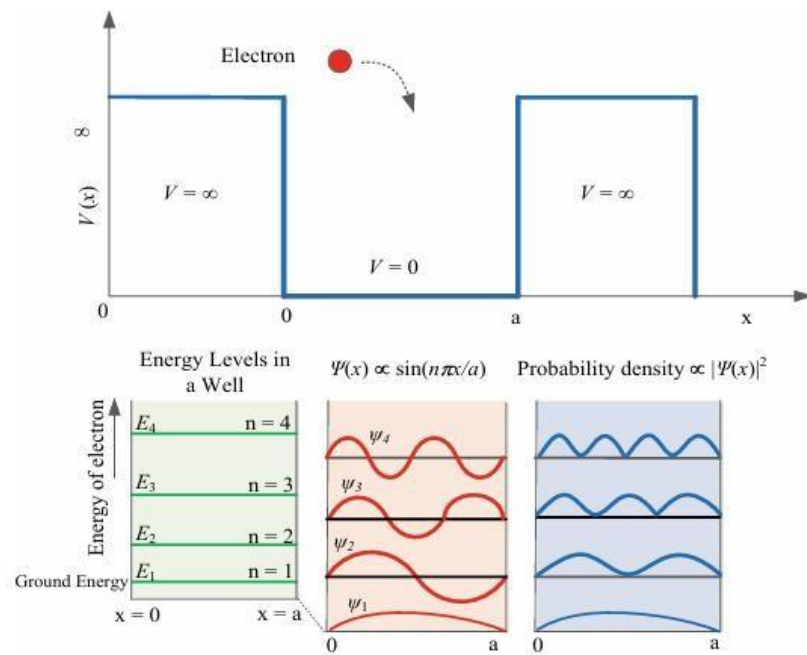
Solution of Schrodinger's equation for this wave function is as  $\sin/\cos$  function, and it also gives the value of the energy of an electron within a potential well. The electron can only have certain discrete energies ( $E_n$ ) matching the allowed wave functions. A lower (higher) energy electron will have a smaller (larger) value of  $k$  (wave vector) and a larger (smaller) wavelength (see Fig. 3.3).

Since the boundary conditions demand the wave function to be zero at the walls of the well, the wave vector can only take discrete quantities and hence the electron can only exist in quantized energy levels. The spacing between adjacent energy levels depends on the width of the potential well. If we consider the height of the potential well as finite, there is a possibility of electrons tunneling out of the potential well. Figure 3.4 shows an example of an electron tunneling across a finite potential well. The potential energy (PE) of point A is less than that of point D. Hence, a car released from point A can at most make it to C but not E.

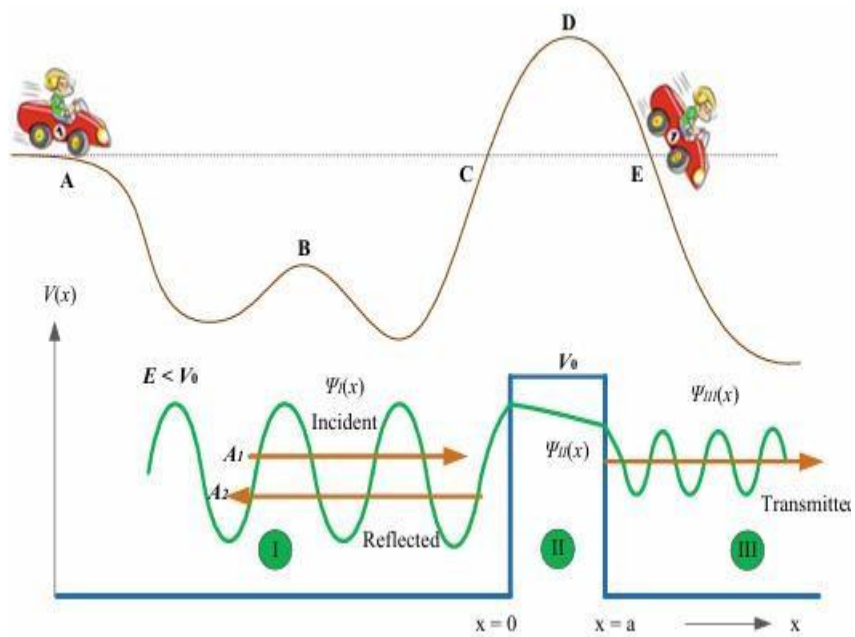
When the car is at the bottom of the hill, its energy is totally kinetic energy (KE). The energy barrier (between C and D) prevents the car from making it to E. In quantum theory, on the other hand, there is a chance that the car could tunnel through (leak) the energy barrier between C and E and emerge on the other side of the hill at E. Figure 3.4 shows the wave function of the electron when it is incident on a PE barrier ( $V_0$ ). The interference of the incident and reflected waves give  $y_I(x)$ .

There is no reflected wave in region III. In region II, the wave function decays with  $x$  because  $E < V_0$ . In quantum theory, on the other hand, there is a chance that the car could tunnel through (leak) the energy barrier between C and E and emerge on the other side of the hill at E. Figure 3.4 shows the wave function of the electron when it is incident on a PE barrier ( $V_0$ ). The interference of the incident and reflected waves give  $y_I(x)$ .

When the car is at the bottom of the hill, its energy is totally kinetic energy (KE). The energy barrier (between C and D) prevents the car from making it to E.

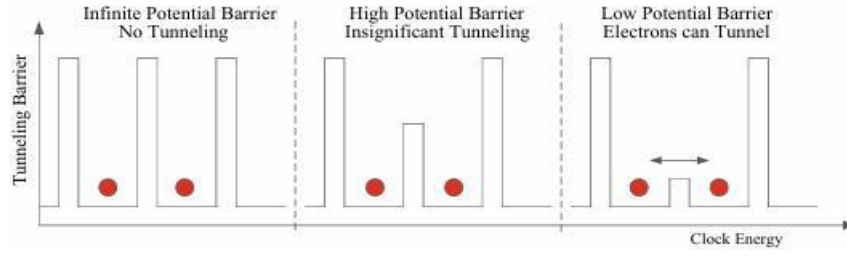


**Fig 4.2: Various quantized energy states of an electron in a one-dimensional infinite potential well. possible wave functions and the probability distributions for the electron are shown**



**Fig 4.3: Roller coaster example for tunneling phenomenon across a finite potential wall**

Solving the Schrodinger equation for the finite barrier region (II) yields an exponential decay function.



**Fig 4.4: Clock energy variation to control the tunneling barrier. while the clock energy given to a qca cell increases, the tunneling barriers lower and allow the electron to tunnel across to the other side.**

This is the main difference to the outer regions of the infinite well, where the wave function must be zero. Solutions for I and III are the same as for the infinite potential well. However, boundary conditions now demand that the wave function matches the exponential function in region II, causing nonzero amplitude in region III.

Since the probability of finding an electron is proportional to the square of the amplitude, therefore, there is an on zero probability to find the electron on the outside, i.e., it can escape from region I. Taking this into account we now look at a simple QCA cell with two electrons placed in neighboring potential wells (called dots). In case of an infinite potential barrier between the dots, electrons are not allowed to tunnel within the dots. As the potential barrier decreases, the possibility of an electron to tunnel across the potential barrier increases.

When the potential barriers are very low, electrons can tunnel freely across the two quantum dots. In QCA technology, clock energy is provided as a means to lower or raise the tunneling barriers as we will see in Sect. 3.6. Figure 3.5 shows how the tunneling barriers between two dots are lowered (raised) when the clock energy supplied to the QCA cell is raised (lowered). The work done in raising and lowering of tunneling barriers controlled by the clock energy can be termed as leakage power dissipation as this will take place even if the QCA cell does not switch state. When the potential barriers are very low, electrons can tunnel freely across the two quantum dots. In QCA technology.

In a similar way, a clock controls the tunneling barriers in a four-dot QCA cell used in this work. Since in practice it is not possible to implement an infinite potential well to prevent the electrons from tunneling across, there is always a finite possibility of

some electronic charge escaping the QCA cell over a long period of time.

However, in this work, we have neglected any loss of charge. Electrons in higher energy states within a potential well are more prone to tunnel across if the tunneling potential is of finite height. Thermal errors are caused when the electrons settle in higher energy orbits and are more likely to tunnel across the barriers as compared to when they are in ground state. A single QCA cell can be modeled by a Hamiltonian of the form. The Hamiltonian of the extended Hubbard type is used to describe a single isolated cell as follow :

$$H^{\text{cell}} = \sum_{i,\sigma} (E_0 + V_i) \hat{n}_{i,\sigma} + \sum_{i>j,\sigma} t_{i,j} \left( \hat{a}_{i,\sigma}^\dagger \hat{a}_{i,\sigma} + \hat{a}_{j,\sigma}^\dagger \hat{a}_{j,\sigma} \right) + \sum_i E_Q \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow} + \sum_{i>j,\sigma,\sigma'} V_Q \frac{\hat{n}_{i,\sigma} \hat{n}_{j,\sigma'}}{|R_i - R_j|} \quad (2.5)$$

This model represents each quantum dot as a site and ignores internal degrees of freedom of the cell. Here,  $E_0$  is the ground state energy for an electron in a single dot,  $n_i$  is the number density for site  $i$ ;  $t_{i,j}$  is the coupling to neighboring dots,  $E_Q$  is the energy to put two electrons on a single dot,  $V_Q$  is the strength of the Coulomb interaction, and the  $R$  are the positions of the dots. The basis states for this Hamiltonian are taken to be states in which each electron is in the ground state of one of the individual dots. This Hamiltonian can be diagonalized directly to determine the two-particle states of the system.

It should be emphasized that Eq. (3.5) is a model in the sense that the strengths of the various terms are put in as constants. The Hamiltonian used to model the cell includes four terms in which the first term represents the on-site energy of each dot. Here, the  $\hat{a}_{i,\sigma}^\dagger$  ( $\hat{a}_{i,\sigma}$ ) is the annihilation (creation) operators for an electron on site  $i$  with spin  $\sigma$ .  $\hat{n}_{i,\sigma}$ , represents the number operator for electrons of spin  $\sigma$  on site  $i$  and  $V_i$  is the potential energy of an electron at dot  $i$  due to charges outside the cell.  $t_{i,j}$  is the tunneling energy between site ' $i$ ' and ' $j$ '. The third terms is the Coulombic cost to put two electrons of opposite spin on a single dot, and the Coulombic interaction between the charge densities on different dots within a cell is calculated in the last term. The stationary state of the cell is given by solving the time-dependent Schrödinger equation.

$$\hat{H}_{\text{cell}} |\psi_i\rangle = E_i |\psi_i\rangle \quad (2.6)$$

where  $|\psi_i\rangle$  and  $E_i$  are the  $i$ th eigen state and eigenvalue of the Hamiltonian, respectively. These eigen state is found using the site-ket basis for the cases of electrons with opposite spin and the 16 possible states as follows:

$$\begin{aligned} |\varphi_1\rangle &= \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\ |\varphi_2\rangle &= \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}, \dots, \\ |\varphi_{16}\rangle &= \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix} \end{aligned} \quad (2.7)$$

Then, the Hamiltonian matrix and its associated eigen vectors will be calculated, in which matrix elements are evaluated as follows:

$$H_{i,j} = \langle \varphi_i | \hat{H} | \varphi_j \rangle \quad (2.8)$$

Here,  $\phi_j$  and  $\psi_0$  are the  $j$ th basis vector and its coefficient, respectively. Coefficient of the basis vector is found by the direct diagonalization of the Hamiltonian matrix. For the case of weak tunneling energy between the sites of the cell (less than the columbic energy), the electrons will remain largely localized and resulting in a polarized cell. If the tunneling energies become comparable to the coulomb energies (more than the coulomb energy), the polarization of the cell is eliminated. In this way, the quantity of the cell polarization is defined as:

$$p = \frac{(\rho_1 + \rho_3) - (\rho_2 + \rho_4)}{\rho_1 + \rho_2 + \rho_3 + \rho_4} \quad (2.10)$$

where  $\rho_i$  denotes the expectation value of the ground state charge configuration as follows:

$$\rho_i = \langle \psi_0 | n_i | \psi_0 \rangle \quad (2.11)$$

We can solve Schrödinger's equation for a system composed of many cells, the ground state of the entire system is found by iteratively solving each cell ground state.

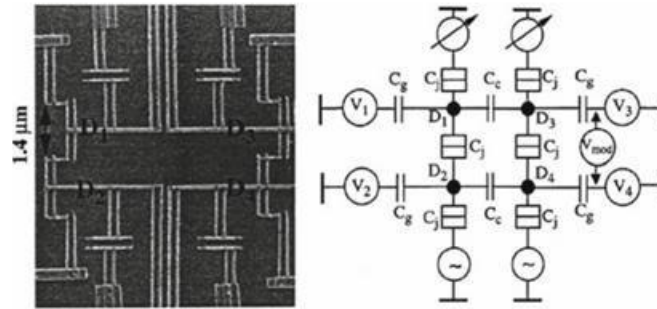
### 4.3 QCA Implementation Techniques

The fundamental component for QCA computation is a bi stable cell capable of interacting with its local neighbors. The cell is not necessarily being in quantum mechanical coherent at all times; as a result, several non-quantum-mechanical realizations of QCA have developed. There are four distinct techniques for physically

implementing QCA:metal-based,semiconductor,molecular,and magnetic . In this section, a brief description of each implementation is provided.

### 4.3.1 Metal Island

Recent works have demonstrated that the metal island-based QCA devices are feasible and work correctly at cryogenic temperature. Metal QCA consists of four metal



**Fig 4.5: Sem image of metal-dot qca cell and corresponding schematic diagram**

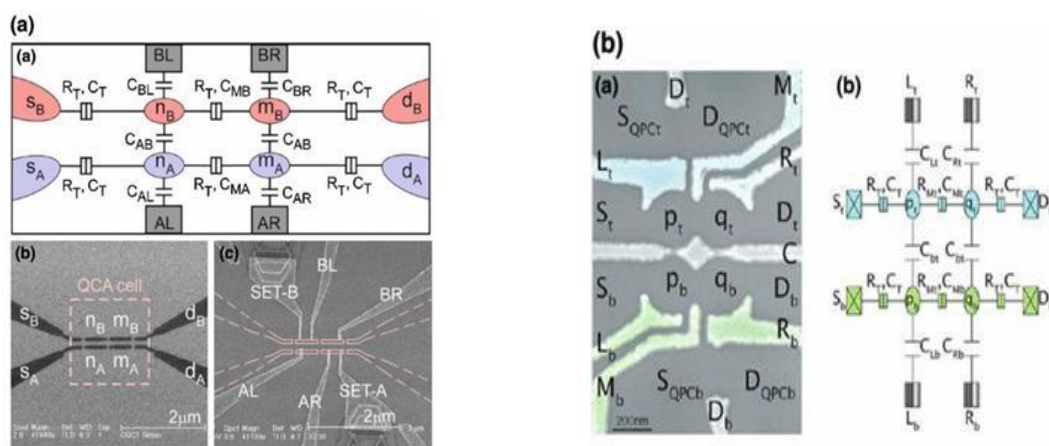
Metal QCA consists of four metal islands, which are relatively large. Metal junction QCA was the first fabrication method considered to show the concept of QCA, where metallic tunnel junctions and very small capacitors are used to build the QCA cells. It was not aimed to compete with the existing technology in terms of speed and practicality, as its structural properties are not suitable for scalable designs. The basic idea of metal-dot QCA is to build quantum dots using aluminum islands. The cell size is approximately 60 nm by 60nm, with junction capacitance of 400 aF . The method has the advantages of an easier fabrication process, reliability, and ease of modeling and analyzing. However, it has one major drawback, which is the operating temperature. The prototype only operates at 10 K or below. The required quantum-mechanical effects only happen at this operating temperature. Metal-dot QCA is meant as a proof-of-concept implementation. In , authors reported a SPICE model development for QCA cells.

### 4.3.2 Semiconductor

Semiconductor QCA implementations can possibly be used to realize QCA devices with the same highly advanced semiconductor fabrication processes used to realize CMOS devices. Semiconductor quantum dots are nano structures formed using electron beam lithographically defined gates on heterostructure materials such as InAs/GaAs and GaAs/AlGaAs .

These structures can be modeled as 3-D quantum wells. Consequently, they show energy

quantization effects even at distances several hundred times larger than the material system lattice constant. Cell polarization is encoded as charge position, and quantum-dot interactions depend on electrostatic coupling. And recently published implementation is based on Silicon (shown in Fig.3.7a). Unfortunately, current semiconductor patterning technologies do not allow for a small enough size scale to make room temperature operation possible. Therefore, semiconductor QCA suffers from the same temperature and speed limitations found with metal-dot QCA. And recently published implementation is based on Silicon (shown in Fig.3.7a). Unfortunately, current semiconductor patterning technologies do not allow for a small enough size scale to make room temperature operation possible.



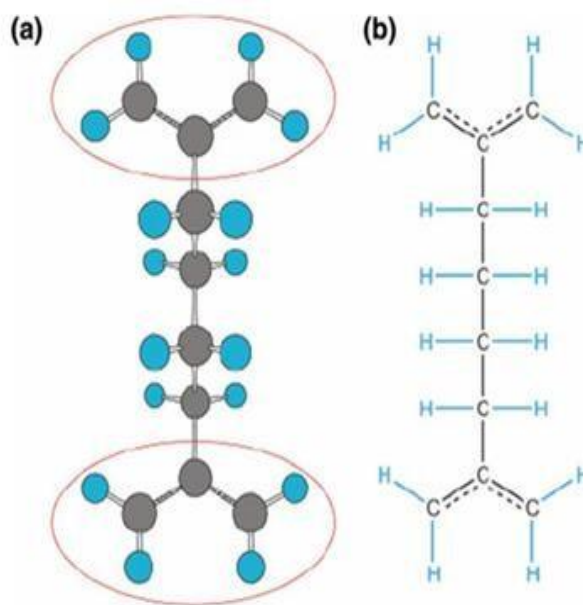
**Fig 4.6: (A) Silicon-based qca schematic and SEM images [18], (b) electron micro graph of a GaAs/AlGaAs QCA cell with simplified circuit equivalent of the four-dot cell**

### 4.3.3 Molecular QCA

Molecular QCA concept consists of building QCA devices out of single molecules. Majority of the work so far has been presented by the research group at Notre Dame. The basic concept of molecular QCA is that each molecular QCA cell consists of a pair of identical allyl groups as shown in and Fig.3.8. The molecule shown in Fig. 3.8 is also known as a 1, 4-diallyl butane radical cation.

These molecules are carefully designed and engineered to exhibit specific electronic properties, allowing them to interact with each other and perform logical operations. By leveraging the unique properties of molecules, molecular QCA has the potential to enable the development of extremely small, fast, and energy-efficient electronic devices, which could revolutionize fields such as computing.

These molecules are carefully designed and engineered to exhibit specific electronic properties, allowing them to interact with each other and perform logical operations.



**Fig 4.7: Two views of molecule as a qca cell**

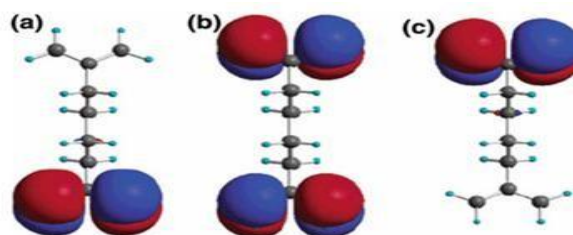
This is formed by two allyl groups connected by a butyl bridge in between. This molecule is neutral on one end and the other end behaves as a cation. This molecule has an extra hole or electron that allows the quantum tunneling effect needed by QCA to happen. If an electrical field is placed near one end of the molecule, it can create either a repelling or attracting force. It has been calculated that the molecule in Fig. 3.8 has nonlinear switching characteristics, which make it an ideal switch.

When the molecules are placed next to each other with a distance of seven angstroms, the electrostatic inter action will cause the holes to be at opposite ends, which makes the propagation of the electron feasible to create the state of the QCA cell. Figure 3.9 shows the different states of the molecular QCA. Part (a) is a +1 state, part (b) is a non-ideal state which is not needed, and part (c) is a -1 state.

At this scale, the required quantum mechanical effects can happen at room temperature. Molecular QCA is believed to have the following advantages: high density, high clock frequency from the giga hertz range to the terahertz range, low power consumption, and low power loss. An individual molecular QCA cell has been demonstrated. However, no complete circuit using molecular QCA has yet been demonstrated. While fabrication methods are currently being researched, no one method has been predominating. Efforts are on to fabricate molecular QCA circuits using self-

assembly mono layer methods. The molecules themselves are produced by standard.

While fabrication methods are currently being researched, no one method has been predominating.



**Fig 4.8: Different possible states of molecule a show a +1state, b show a non-ideal state that is a unwanted state, and c show a -1state**

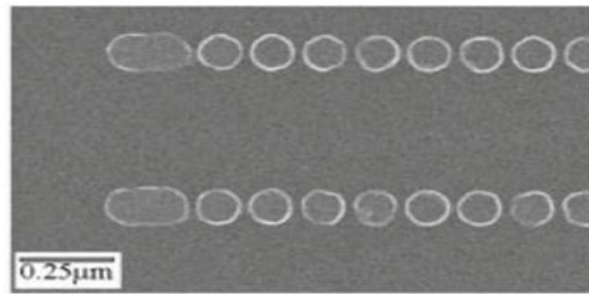
#### 4.3.4 Magnetic QCA

A basic cell in magnetic QCA is a nano magnet. These nano magnets are arranged in various grid-like fashions to accomplish computing. Cells in magnetic QCA are enumerated based on their single-domain magnetic dipole moments and are inherently energy minimums.

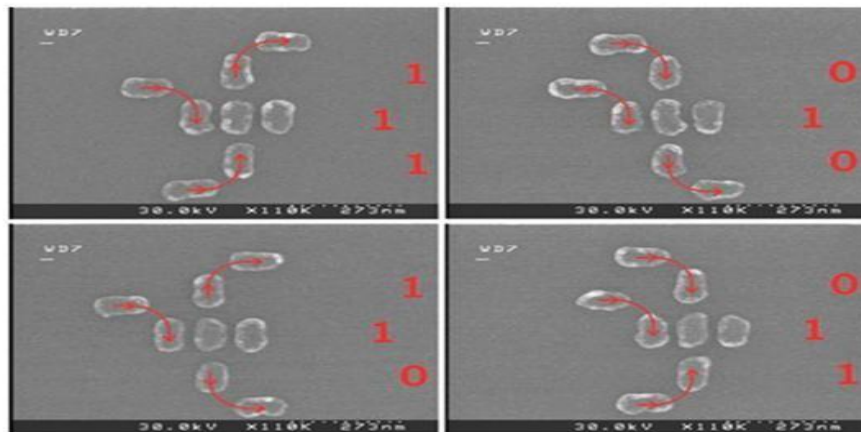
There are several popular schemes of magnetic QCA that have been proposed: Cow burn and Wellands nano dot QCA Automata , Parish and For shaws Bi stable Magnetic QCA , and Csabaetal., Field Couple Nano magnets . Cow burn and Wellands have fabricated the magnetic QCA model that has been described here. A nano magnet consists of a single circular nano dot. Cells in magnetic QCA are enumerated based on their single-domain magnetic dipole moments and are inherently energy minimums.

These nanodots were made of a magnetic Superalloy (mainly Ni). The nano dots are 110 nm in diameter and had a thickness of 10 nm. In order to have a single domain in the nano dots, it was found that the nano dots must have a size of about 100 nm and below. Nano dots are placed 20 nm apart on a straight line. The basic operation is to use an oscillating field on the dot to have it point to a certain direction to represent the binary value. Magnetic QCA cell is capable of operating at room temperature. Other advantages include high density and low power loss. The operating frequency is low (in the MHz range) when compared to CMOS. ANOT gate and a majority gate have been demonstrated. Figure 3.10 shows a SEM image of a fabricated magnetic QCA network. Figure 3.11 shows the implementation of a majority gate using nanodots by Imre et al. Nano dots are placed 20 nm apart on a straight line. The basic operation is to use an oscillating

field on the dot to have it point to a certain direction to represent the binary value. Other advantages include high density and low power loss.



**Fig 4.9: Sem image of a room temperature mqca network**



**Fig 4.10: Implementations of a majority gate for magnetic quantum-dot cellular automata. the arrows drawn super imposed on the sem images illustrate the resulting magnetization direction due to a horizontally applied external clock field.**

## 4.4 QCA Devices

This section explains the basic operation of QCA technology and its associated components, such as a cell, wire, majority gate, and inverter. The layout designs of the QCA circuits are the combination of all the mentioned components. Two different QCA structures of the fundamental gates are illustrated in Figs. 3.12a, b, namely the inverter (INV) and the majority gate (MV). In addition, Fig. 3.12c shows cascade of QCA cells to propagate binary data which represents a QCA wire. The 3-input majority gate function is described by the following equation:

$$MV3(A,B,C) = F = AB+BC+CA \quad (2.12)$$

## 4.5 QCA Clocking

In traditional VLSI technology, clocking mechanism is used to control the timing in sequential circuits. In QCA technology, a pipeline-based clock mechanism is essentially required for both sequential and combinational designs. This mechanism not only controls the data flow, but also supplies power for the cells. For the clocking purpose, four clocks are applied, i.e., clock 0, clock 1, clock 2, and clock 3.

Quantum dot cellular automata (QDCA, sometimes referred to simply as quantum cellular automata, or QCA) are a proposed improvement on conventional computer design (CMOS), which have been devised in analogy to conventional models of cellular automata introduced by John von Neumann. These clocks are  $90^\circ$  out of phase as apparent in Fig. 3.13. Each clock in QCA comprises of four distinct clock phases: switch, hold, release, and relax as depicted in Fig.3.13.

In switch state, cells start polarized and inter-dot barriers are raised and QCA cell attends one of the polarization states depending on the state of driving cell. During this phase, the real computation occurs. During the hold phase, cells have a fixed polarization to drive the succeeding stage. In the release phase, cells start unpolarized and during the final stage, inter-dot barriers stay lowered and a cell has no fixed polarization. These clocks are  $90^\circ$  out of phase as apparent in Fig. 3.13. Each clock in QCA comprises of four distinct clock phases: switch, hold, release, and relax as depicted in Fig.3.13.

Quantum dot cellular automata (QDCA, sometimes referred to simply as quantum cellular automata, or QCA) are a proposed improvement on conventional computer design (CMOS), which have been devised in analogy to conventional models of cellular automata introduced by John von Neumann.

Quantum-dot Cellular Automata (QCA) clocking is a crucial aspect of QCA circuit design, as it enables the synchronization of information flow and computation within QCA circuits. In QCA clocking, a clock signal is applied to the QCA cells to control the flow of information and to synchronize the computation process. The clock signal is typically applied in a four-phase clocking scheme, which includes four distinct phases: switch, hold, release, and relax. During each phase, the QCA cells are either allowed to switch, hold their state, release their state, or relax to their ground state. By carefully controlling the clock signal and the four-phase clocking scheme, QCA clocking Other advantages include high density and low power loss.

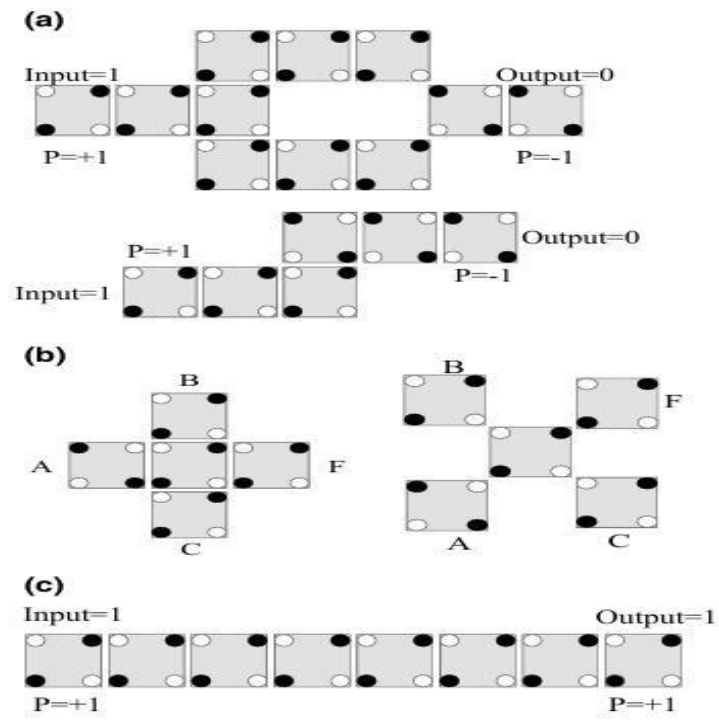


Fig 4.11: Qca primitives: (a) two different realizations of inverter, (b) original majority gate (omg) and rotated majority gate (rmg), and (c) qca wire.

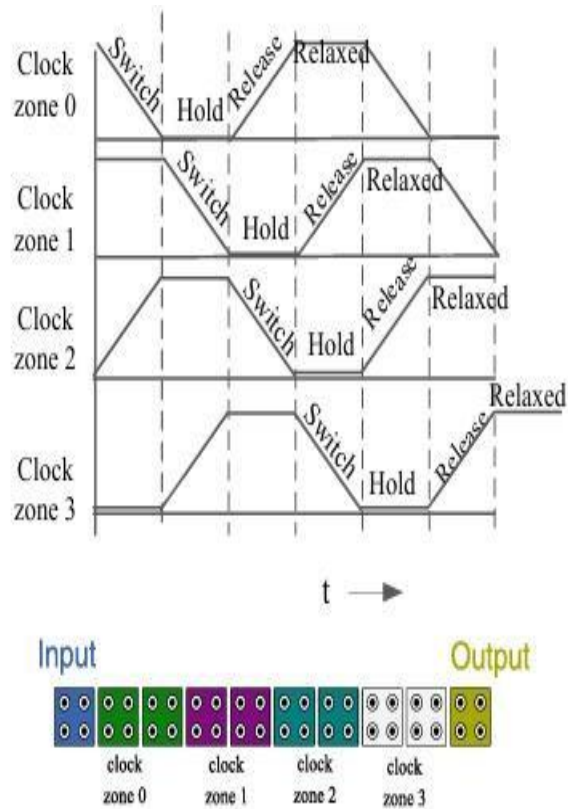
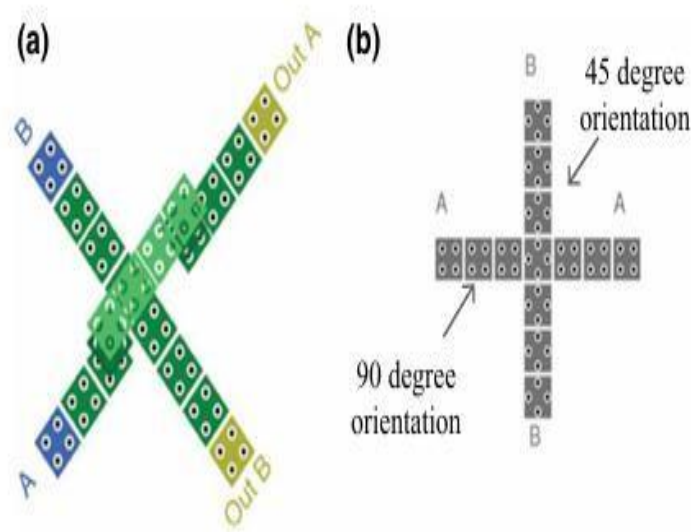


Fig 4.12: Qca clocking with four phases

## 4.6 QCA Wire Crossing

In QCA structures, fabrication of interconnection between components needs to be handled efficiently for a better stability. Till date, there are two different types of crossover methods commonly utilized, coplanar and multilayer. The multilayer crossover uses more than one layer of cells (analogous to multiple metal layers in a conventional IC), shown in Fig. 3.14a but yields high cost due to, for instance, fabrication issue . In coplanar crossover strategy, wire crossing is done by two different cells.

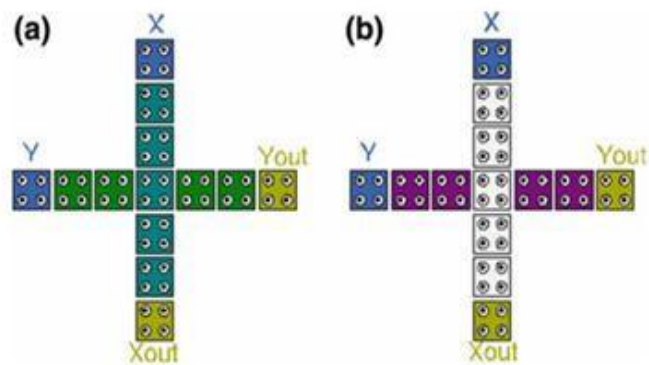
These cells are orthogonal to each other, so they operate without affecting neighboring cells. The first wire consists of cells of  $90^\circ$  orientations and second wire has only  $45^\circ$  orientations, as depicted in Fig. 3.14b. The main drawback of this scheme is that any misalignment of cells during fabrication may cause a cross-coupling between the two wires. Works have been done to mitigate such effects and to increase the robustness of the circuits, but all these ends up with large area overhead .



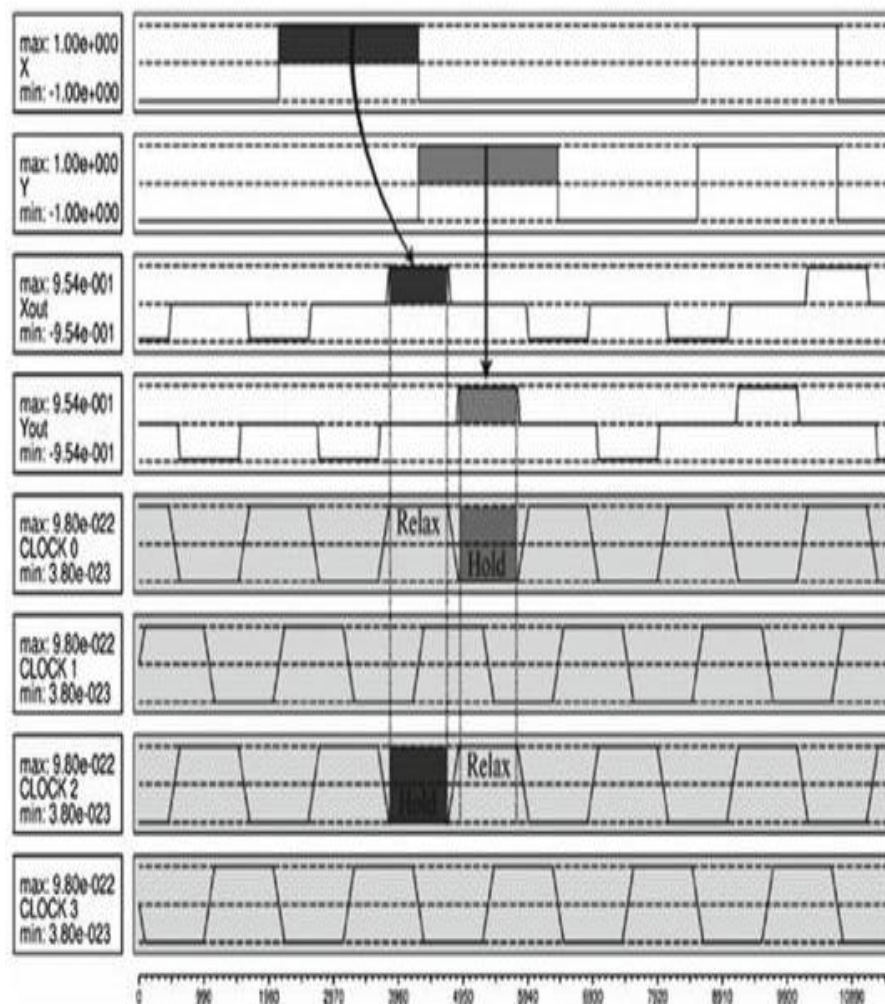
**Fig 4.13: Wire crossing a multilayer and b coplanar**

In this work, wire crossing utilizes clock zone-based crossover where cells on the switch phase can cross cells on the release phase and cells on the hold phase cross cells on the relax phase without polarization effect as depicted in Fig. 3.15a, b, respectively. This scheme takes advantage of two zones of the four phase zone-based clocking scheme. For illustrations of Fig. 3.15b, the input/output signals with a fore mentioned clocking correspond to Clock 0, and Clock 2 are shown in Fig. 3.16, which is identically produced by Coherence vector and Bistable simulation.

The multilayer crossover uses more than one layer of cells



**Fig 4.14: Wire crossing using clock zone (a) cells on the switch phase cross cells on the release phase and (b) cells on the hold phase cross cells on the relax phase**



**Fig 4.15: I/O and clocking signals for clock zone-based crossover**

This figure also indicates that the relax and hold phases of Clock0 coincide with the hold and relax phases of Clock2, respectively. Works have been done to mitigate such effects and to increase the robustness of the circuits, but all these ends up with large area overhead. In this work, wire crossing utilizes clock zone-based crossover where cells on the switch phase can cross cells on the release phase and cells on the hold phase cross cells on the relax phase without polarization effect. Therefore, when the central cell is clocked by Clock2 (Clock0), signal X (Y) passes through.

#### 4.6.1 Kink Energy and Cell Robustness

In QCA implementation of larger designs, designers are more concerned about increasing robustness/stability of whole QCA structure. As the wire length increases, the switching probability of QCA cell decreases; similarly, QCA cell switches successfully for smaller wire length. Moreover, the circuits operate at higher clock rates. It has been experimentally shown that the number of cells in a wirelength for healthy transmission of a signal is 28 (90°) or 27 (45°). At higher operating temperatures, due to thermal fluctuation, the QCA cell characteristic deviates, i.e., a kink to occur. To avoid kinks, the maximum number of cells is given by

$$N \leq e^{E_k/kbT} \quad (2.13)$$

where  $E_k$  is the kink energy,  $kb$  is Boltzmann's constant and operating temperature  $T$ .

#### 4.7 Modeling QCA Designs

There are several approximate simulators available at the layout level, such as the bistable simulation engine and the nonlinear approximation methods. The coherence vector-based method does explicitly estimate the polarizations, but it is appropriate when one needs full temporal dynamics simulation (Bloch equation), and hence is extremely slow. Coherence vector simulations are generally accepted as the most accurate simulation engine for clocked QCA due to the quantum mechanical properties which are integrated in the simulations. They also provide information on power, speed, and reliability and include temperature and other electrical properties. QCADesigner is an easy and useful program to design and simulate QCA circuits. QCADesigner is not just a switch-level simulator. It simulates QCA using the quantum mechanics of QCA.

Modeling QCA (Quantum-dot Cellular Automata) designs involves creating simulations and representations of how QCA cells interact and perform computations. Here's a brief overview:

1. **Cell Structure:** QCA cells are typically bistable, meaning they have two stable states. These cells are coupled through electrostatic forces.
2. **Molecular vs. Magnetic QCA:** There are two main types of QCA implementations. Molecular QCA uses complex molecules with oxide-reduction centers, while magnetic QCA uses nanometer-sized magnets with two stable magnetic states (up and down).
3. **Simulation:** To model QCA designs, simulations are run to observe how cells interact and how information propagates through the system. This helps in understanding the behavior of QCA circuits and optimizing their design.
4. **Design Constraints:** When modeling QCA designs, it's important to consider technological constraints and ensure that the designs are feasible with current technology.
5. **Applications:** QCA designs have potential applications in creating circuits with extremely low power consumption and intrinsic memory capabilities

In QCA, there are two primary implementations: molecular QCA and magnetic QCA. Molecular QCA uses complex molecules that have redox centers capable of holding binary states, while magnetic QCA utilizes nanoscale magnets that maintain two stable magnetic states (up and down). When designing and modeling QCA circuits, simulations play a crucial role. These simulations help in visualizing how the cells will interact, how information will propagate through the system, and how the design will perform in real-world conditions.

The constraints in designing QCA systems are often technological, requiring careful consideration to ensure that the designs are practical and feasible with the current state of technology. One significant advantage of QCA designs is their potential for extremely low power consumption and inherent memory capabilities, making them a promising area for future technological advancements in various applications, including nano electronics and efficient computing systems.

Molecular QCA uses complex molecules that have redox centers capable of holding binary states, while magnetic QCA utilizes nanoscale magnets that maintain two stable magnetic states (up and down). When designing and modeling QCA circuits, simulations play a crucial role. These simulations help in visualizing how the cells will interact, how information will propagate through the system, and how the design will perform in real-world conditions.

**Table 4.1: Bistable approximation and coherence vector parameters model**

<b>Parameter</b>	<b>Bistable approximation</b>	<b>Coherence vector</b>
Number of samples	12,800	12,800
Convergence tolerance	0.001000	-
Radius of effect	65 nm	80 nm
Relative permittivity	12.9	12.9
Clock high	9.8e-22J	9.8e-22J
Clock low	3.8e-23J	3.8e-23J
Clock amplitude factor	2	2
Layer separation	11.500 nm	11.500 nm
Maximum iterations per sample	100	-
Relaxation time	-	4.135e-14s
Time step	-	1e-016 s
Total simulation time	-	7e-011 s

Simulation engine has two choices, coherence vector and bistable. The simulation type is to allow the user to set up the input test vectors. All the simulations were done in QCADesigner v2.0.3 using bistable approximation and coherence vector simulation engine. The parameters of the simulation are the default values used by QCADesigner as shown in Table 3.1.

#### 4.7.1 QCA Power Dissipation Model

Work by Timler and Lent initially developed a power estimation model for QCA based circuit. A Hamiltonian matrix is used to measure energy related to a QCA cell. By considering Hartree–Fock approximation and mean-field approach, Coulombic interaction between QCA cells, and the Hamiltonian matrix for an array of cell is expressed as

$$H = \begin{bmatrix} -\frac{E_k}{2} \sum_i c_i f_{ij} & -\gamma \\ -\gamma & \frac{E_k}{2} \sum_i c_i f_{ij} \end{bmatrix} = \begin{bmatrix} -\frac{E_k}{2} (C_{j,1} + C_{j+1}) & -\gamma \\ -\gamma & \frac{E_k}{2} (C_{j,1} + C_{j+1}) \end{bmatrix} \quad (2.14)$$

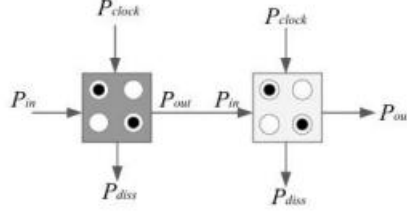
Where  $f_{ij}$  is a geometrical factor representing electrostatic interactions between cell  $i$  and cell  $j$  due to the geometrical distance and polarization of the  $i$ th juxtaposed cell is represented by  $C_i$ . If the space between neighboring cells are equal, then  $f_{ij}$  is interpreted as the kink energy, which can be calculated using the electrostatic interaction between all electrons in two cells,  $i$  and  $j$ , as

$$E_{ij} = \frac{1}{4\pi\epsilon_0\epsilon_r} \sum_{n=1}^4 \sum_{m=1}^4 \frac{q_{i,n} q_{j,m}}{|r_{i,n} - r_{j,m}|} \quad (2.15)$$

At each clock cycle, the expectation value of QCA cell energy is expressed as

$$E = \langle H \rangle = \frac{\hbar}{2} \cdot \vec{\Gamma} \cdot \vec{\lambda} \quad (2.16)$$

where  $E = \hbar \omega$  is the Planck constant,  $\vec{\Gamma}$  is the energy environment vector of the cell, and coherence vector is represented as  $\vec{\lambda}$ . The Hamiltonian vector is presented as



**Fig 4.16: Power flows between two qca cells**

$$\vec{\Gamma} = \frac{1}{\hbar} [-2\gamma, 0, E_k(C_{j-1} + C_{j+1})] \quad (2.17)$$

Here,  $(C_{j-1} + C_{j+1})$  represents the sum of neighboring polarizations. Power flow between neighboring cells is shown in Fig. 2.17. As mentioned in ,  $P_{in}$  and  $P_{out}$  are the inflow signal power and the released signal power for a QCA cell. During the switch phase,  $P_{clock}$  amount of energy transfer to the cell as inter-dot barriers are raised. Similarly, in the release phase, the energy gets returned to the clocking circuit as barriers are reduced. During this process, a small power is dissipated in the clocking circuit named as  $P_d$ . The total instantaneous power for a cell is given as

$$P_t = \frac{dE}{dt} = \frac{\hbar}{2} \left[ \frac{d\vec{\Gamma}}{dt} \cdot \vec{\lambda} \right] + \frac{\hbar}{2} \left[ \vec{\Gamma} \cdot \frac{d\vec{\lambda}}{dt} \right] = P_1 + P_2 \quad (2.18)$$

where  $P_1$  combines the difference of input and output signal powers and clocking power to the cell. The term  $P_1$  can be written:

$$P_1 = P_{in} - P_{out} + P_{clock} \quad (2.19)$$

Here,  $P_{clock}$  is the amount of transferred energy into the cell by the clock,  $P_{in}$  is the signal power in from the left side cell, and  $P_{out}$  is the signal power out to the right side cell. The power gain of each cell is then:

$$\text{gain} = P_{\text{out}} / P_{\text{in}} \quad (2.20)$$

The term  $P_2$  is the cell dissipated power to the environment. In QCA circuits, power consumption occurs in each cell during a quasi-adiabatic clocking scheme. It is not worthy that a considerable amount of energy is transferred to the cell as the barriers are being raised. Most of that energy is returned to the clock as the barriers are being lowered. The difference between these two amounts is the consumed power which is categorized into two types: switching and leakage powers.

The switching power occurs when the cell actually changes the state from '0' to '1' or inversely. Leakage power is dependent on the clock energy changing to polarize or depolarize a cell. According to, the Hamiltonian and coherence vectors can be used to calculate the energy dissipation in one clock cycle  $T_{\text{cc}} = [-T, T]$  as

$$E_{\text{diss}} = \frac{\hbar}{2} \int_{-\pi}^T \vec{\Gamma} \cdot \frac{d\vec{\lambda}}{dt} dt = \frac{\hbar}{2} \left( \left[ \vec{\Gamma} \cdot \vec{\lambda} \right]_{-T}^T - \int_{-T}^T \vec{\lambda} \cdot \frac{d\vec{\Gamma}}{dt} dt \right) \quad (2.21)$$

The upper bound power dissipation mode line is presented as

$$P_{\text{diss}} = \frac{E_{\text{diss}}}{T_{\text{cc}}} < \frac{\hbar}{2T_{\text{cc}}} \vec{\Gamma}_+ \times \left[ -\frac{\vec{\Gamma}_+}{|\vec{\Gamma}_+|} \tanh\left(\frac{\hbar |\vec{\Gamma}_+|}{k_B T}\right) + \frac{\vec{\Gamma}_-}{|\vec{\Gamma}_-|} \tanh\left(\frac{\hbar |\vec{\Gamma}_-|}{k_B T}\right) \right] \quad (2.22)$$

Here,  $\Gamma_+$  and  $\Gamma_-$  represent  $\Gamma(+T)$  and  $\Gamma(-T)$ , respectively,  $k_B$  defines the Boltzmann constant, and  $T$  is the temperature. Authors in addressed a power dissipation model by considering above concepts and developed a power estimation tool known as QCAPro. This helps to evaluate the total power loss in a QCA circuit as a combination of leakage and switching power when clock changes. It is not worthy that a considerable amount of energy is transferred to the cell as the barriers are being raised. Authors in addressed a power dissipation model by considering above concepts and developed a power estimation tool known as QCAPro. Authors in addressed a power dissipation model by considering above concepts and developed a power estimation tool known as QCAPro.

## **4.8 Summary**

An overview of QCA devices and associated logic circuits are explained in this chapter. It includes basics of QCA, comprehensive review from the literature, various types of implementation techniques along with clocking, and wire crossing mechanisms. It is not worthy that a considerable amount of energy is transferred to the cell as the barriers are being raised. Most of that energy is returned to the clock as the barriers are being lowered. The difference between these two amounts is the consumed power which is categorized into two types: switching and leakage powers. A brief discussion of various types of design and simulation tools is also provided.

## **CHAPTER 5**

### **QCA ADDERS**

#### **5.1 FULL ADDER**

A full adder is a digital circuit that performs the addition of three one-bit binary numbers. It's a fundamental component in digital electronics and computer architecture. The full adder takes three inputs: A (first bit), B (second bit), and Cin (carry-in bit). These inputs are then processed to produce two outputs: Sum (result of the addition) and Cout (carry-out bit).

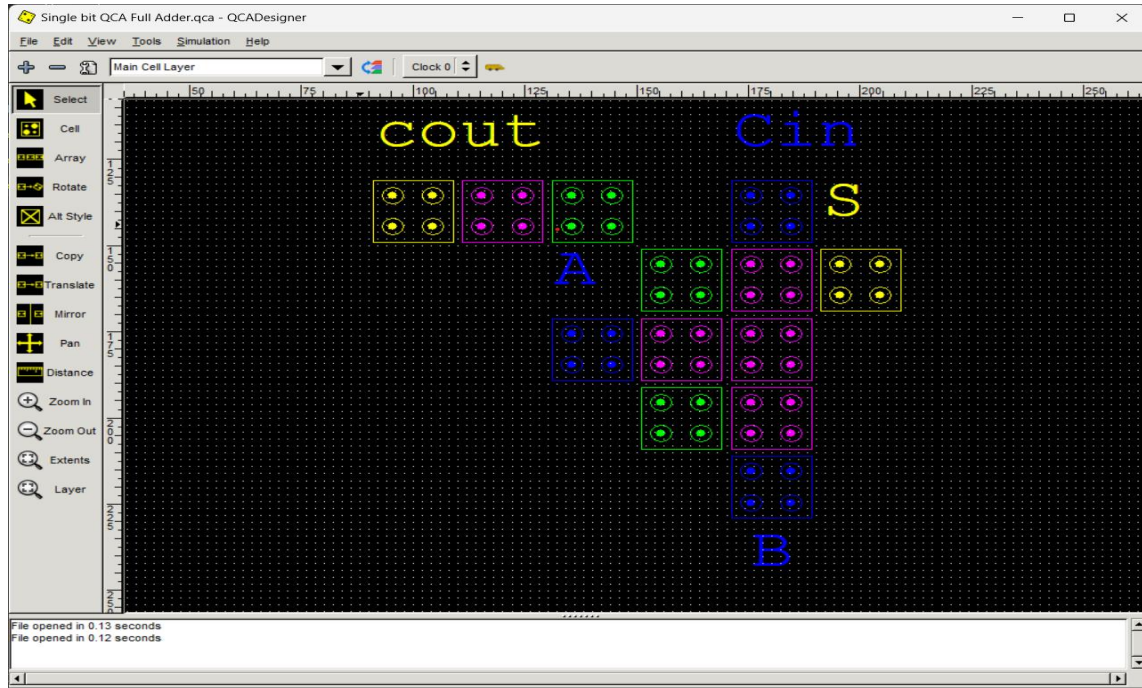
The full adder's functionality can be explained by considering the possible combinations of its inputs. When all inputs are 0, the Sum output is 0 and the Cout output is 0. When the inputs are a combination of 0s and 1s, the Sum and Cout outputs change accordingly. For instance, when A and B are 1 and Cin is 0, the Sum output is 0 and the Cout output is 1. This process continues for all possible input combinations.

A full adder using Quantum-dot Cellular Automata (QCA) is a revolutionary approach to binary addition. QCA is a technology that uses quantum dots to represent binary information, offering a potential replacement for traditional transistor-based computing. A QCA full adder can be designed using a combination of QCA cells, which are the basic building blocks of QCA circuits. Each QCA cell consists of four quantum dots that can be polarized to represent binary information. The QCA full adder design involves QCA cells, QCA wires, and QCA majority gates. QCA wires connect the cells and transmit binary information, while QCA majority gates perform logical operations like AND and OR. The QCA full adder truth table is identical to the traditional full adder truth table, ensuring accurate binary addition.

The QCA full adder offers several advantages, including low power consumption, high scalability, and high speed. QCA circuits consume significantly less power compared to traditional transistor-based circuits, making them ideal for high-density computing applications. Additionally, QCA circuits can be scaled down to smaller sizes and operate at high speeds, making them suitable for high-performance computing applications.

The QCA full adder design involves QCA cells, QCA wires, and QCA majority gates. QCA wires connect the cells and transmit binary information, while

QCA majority gates perform logical operations like AND and OR.



**Fig 5.1: Full adder layout using qca designer 2.0.3**

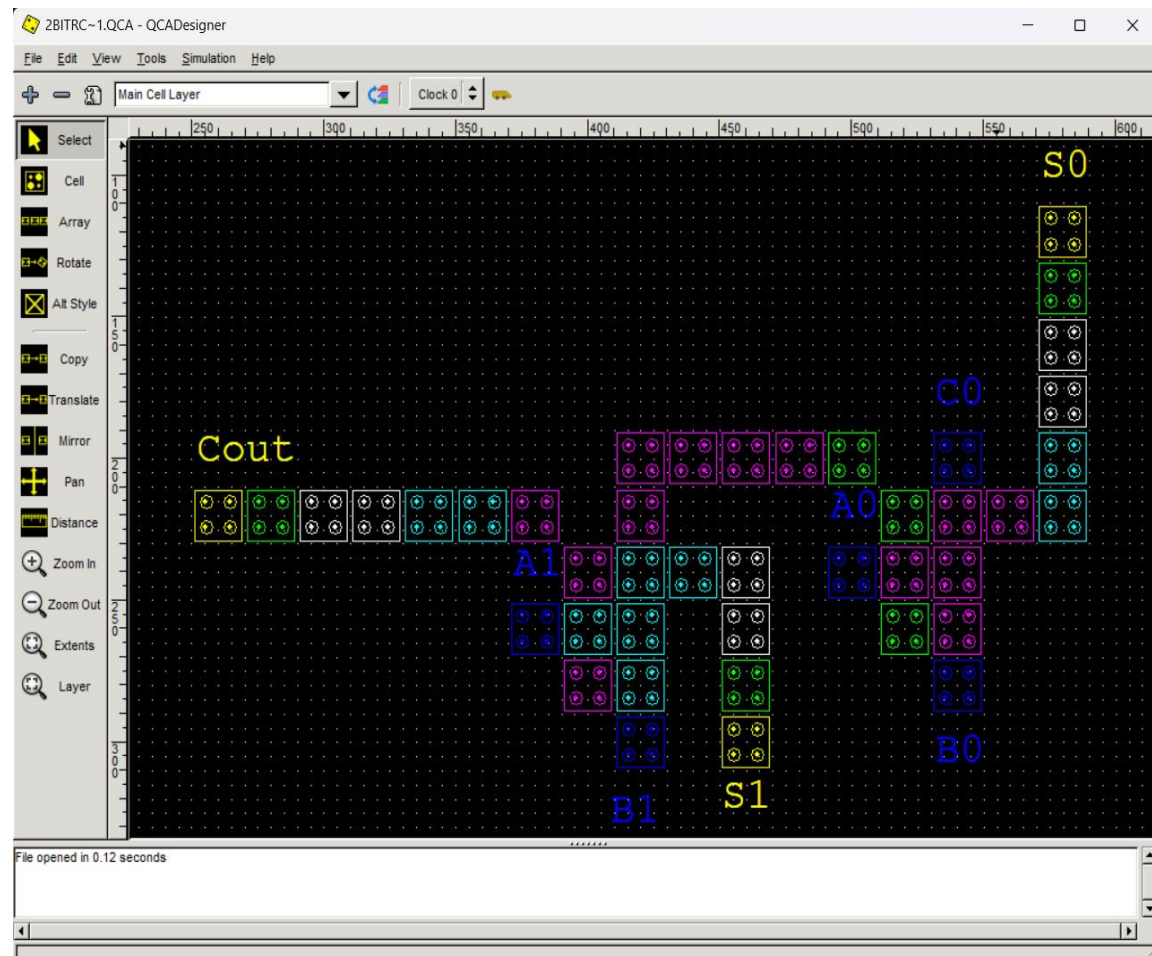
## 5.2 2-BIT RIPPLE CARRY ADDER

A 2-bit ripple carry adder is a digital circuit that adds two 2-bit binary numbers. It consists of two full adders connected in a cascade, allowing it to add the two input numbers bit by bit. The first full adder adds the least significant bits (A0 and B0) of the two input numbers and produces a sum (S0) and carry (C0) output.

The carry output (C0) from the first full adder is then connected to the carry input of the second full adder. The second full adder adds the most significant bits (A1 and B1) of the two input numbers along with the carry output (C0) from the first full adder. This produces a sum (S1) and carry (C2) output. The final output of the 2-bit ripple carry adder is the sum (S1S0) and carry (C2) bits.

A 2-bit ripple carry adder using Quantum-dot Cellular Automata (QCA) is a revolutionary approach to binary addition. QCA is a technology that uses quantum dots to represent binary information, offering a potential replacement for traditional transistor-based computing. The 2-bit QCA ripple carry adder consists of two QCA full adders connected in a cascade, allowing it to add two 2-bit binary numbers bit by bit. The 2-bit QCA ripple carry adder offers several advantages, including low power consumption, high scalability, and high speed.

QCA circuits consume significantly less power compared to traditional transistor-based circuits, making them ideal for high-density computing applications. The first QCA full adder adds the least significant bits (A0 and B0) of the two input numbers and produces a sum (S0) and carry (C0) output. The carry output (C0) is then connected to the carry input of the second QCA full adder. The second QCA full adder adds the most significant bits (A1 and B1) of the two input numbers along with the carry output (C0) from the first QCA full adder. This produces a sum (S1) and carry (C2) output.



**Fig 5.2 : 2-Bit rca layout using qca designer 2.0.3**

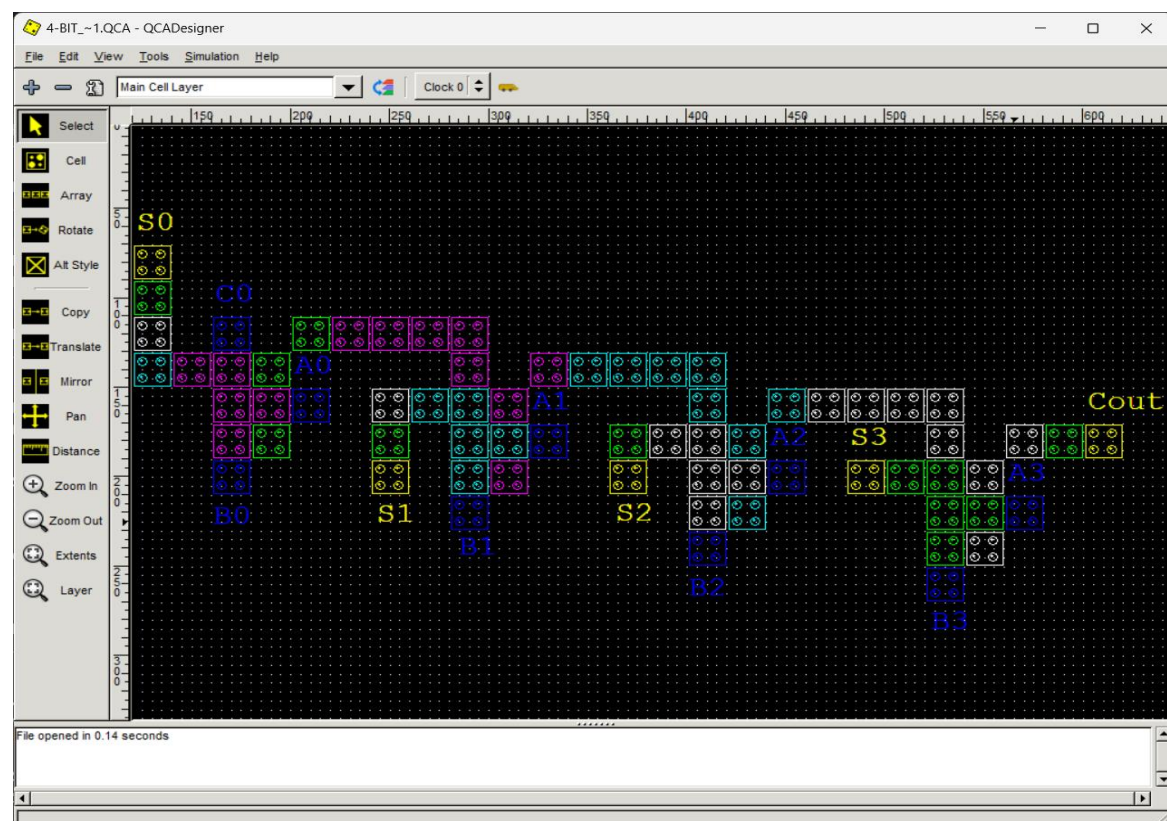
### 5.3 4-BIT RCA

A 4-bit ripple carry adder (RCA) is a digital circuit that adds two 4-bit binary numbers. It consists of four full adders connected in a cascade, allowing it to add the two input numbers bit by bit. The first full adder adds the least significant bits (A0 and B0) of the two input numbers and produces a sum (S0) and carry (C0) output. The carry output (C0) from the first full adder is then connected to the carry input of the second full adder. The second full adder adds the next significant bits (A1 and B1) of the two

input numbers along with the carry output (C0) from the first full. This produces a sum (S1) and carry (C1) output. The process continues for the remaining two bits, with each full adder adding the corresponding bits of the input numbers and the carry output from the previous full adder. The final output of the 4-bit RCA is the sum (S3S2S1S0) and carry (C3) bits. The 4-bit RCA operates according to its truth table, which defines the output for each possible combination of inputs.

A 4-bit ripple carry adder (RCA) using Quantum-dot Cellular Automata (QCA) is a revolutionary approach to binary addition. QCA is a technology that uses quantum dots to represent binary information, offering a potential replacement for traditional transistor-based computing. The 4-bit QCA RCA consists of four QCA full adders connected in a cascade, allowing it to add two 4-bit binary numbers bit by bit.

Each QCA full adder adds the corresponding bits of the input numbers and the carry output from the previous full adder, producing a sum and carry output. The QCA full adders are designed using QCA cells, which are the basic building blocks of QCA circuits. The QCA cells are connected by QCA wires, which transmit binary information, and QCA majority gates, which perform logical operations. The 4-bit QCA RCA operates according to its truth table, which defines the output for each possible combination of inputs.



**Fig 5.3 : 4-Bit rca layout using qca designer 2.0.3**

## 5.4 8-BIT RCA

An 8-bit ripple carry adder (RCA) is a digital circuit that adds two 8-bit binary numbers. It consists of eight full adders connected in a cascade, allowing it to add the two input numbers bit by bit. The first full adder adds the least significant bits (A0 and B0) of the two input numbers and produces a sum (S0) and carry (C0) output. The 8-bit RCA operates according to its truth table, which defines the output for each possible combination of inputs. The truth table ensures accurate binary addition and allows the circuit to produce the correct sum and carry outputs for any given input.

The carry output (C0) from the first full adder is then connected to the carry input of the second full adder, which adds the next significant bits (A1 and B1) of the two input numbers along with the carry output (C0) from the first full adder. This process continues for the remaining six bits, with each full adder adding the corresponding bits of the input numbers and the carry output from the previous full adder. The final output of the 8-bit RCA is the sum (S7S6S5S4S3S2S1S0) and carry (C7) bits.

An 8-bit ripple carry adder (RCA) using Quantum-dot Cellular Automata (QCA) is a revolutionary approach to binary addition. QCA is a technology that uses quantum dots to represent binary information, offering a potential replacement for traditional transistor-based computing. The 8-bit QCA RCA consists of eight QCA full adders connected in a cascade, allowing it to add two 8-bit binary numbers bit by bit.

Each QCA full adder is designed using QCA cells, which are the basic building blocks of QCA circuits. The QCA cells are connected by QCA wires, which transmit binary information, and QCA majority gates, which perform logical operations. The QCA full adders add the corresponding bits of the input numbers and the carry output from the previous full adder, producing a sum and carry output. The 8-bit QCA RCA operates according to its truth table, which defines the output for each possible combination of inputs.

The QCA full adders add the corresponding bits of the input numbers and the carry output from the previous full adder, producing a sum and carry output. The 8-bit QCA RCA operates according to its truth table, which defines the output for each possible combination of inputs. The 8-bit QCA RCA operates according to its truth table, which defines the output for each possible combination of inputs.

The 8-bit QCA RCA operates according to its truth table, which defines the output for

each possible combination of inputs.

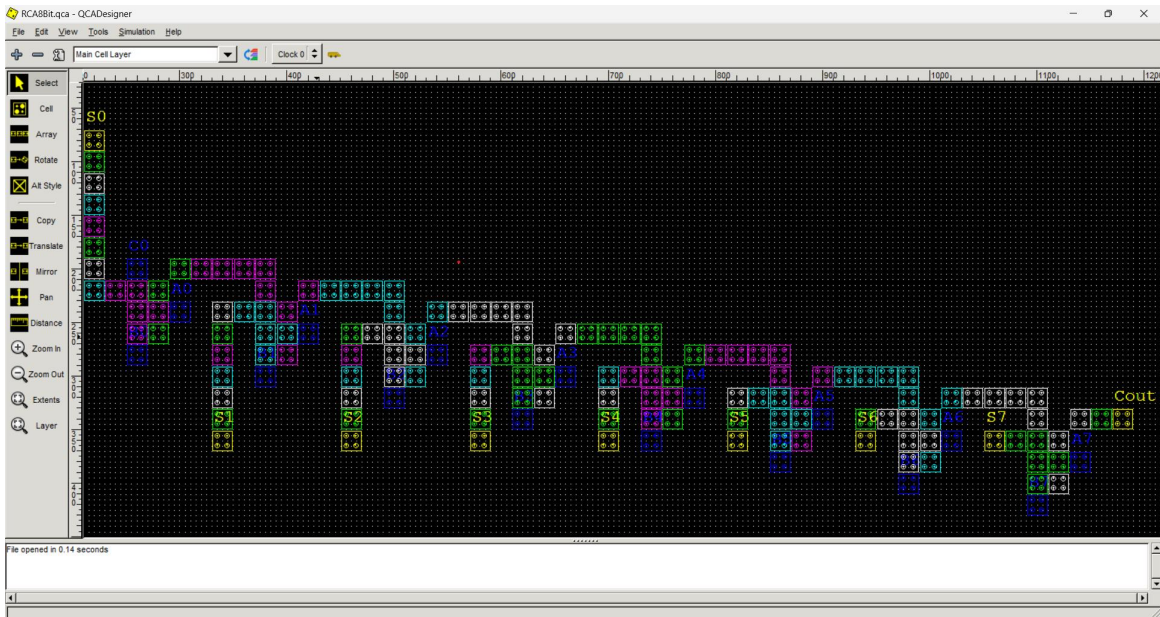


Fig 5.4 : 8-Bit rca latout using qca designer 2.0.3

# CHAPTER 6

## RESULTS

### 6.1 SIMULATION RESULTS

#### 1. FULL ADDER

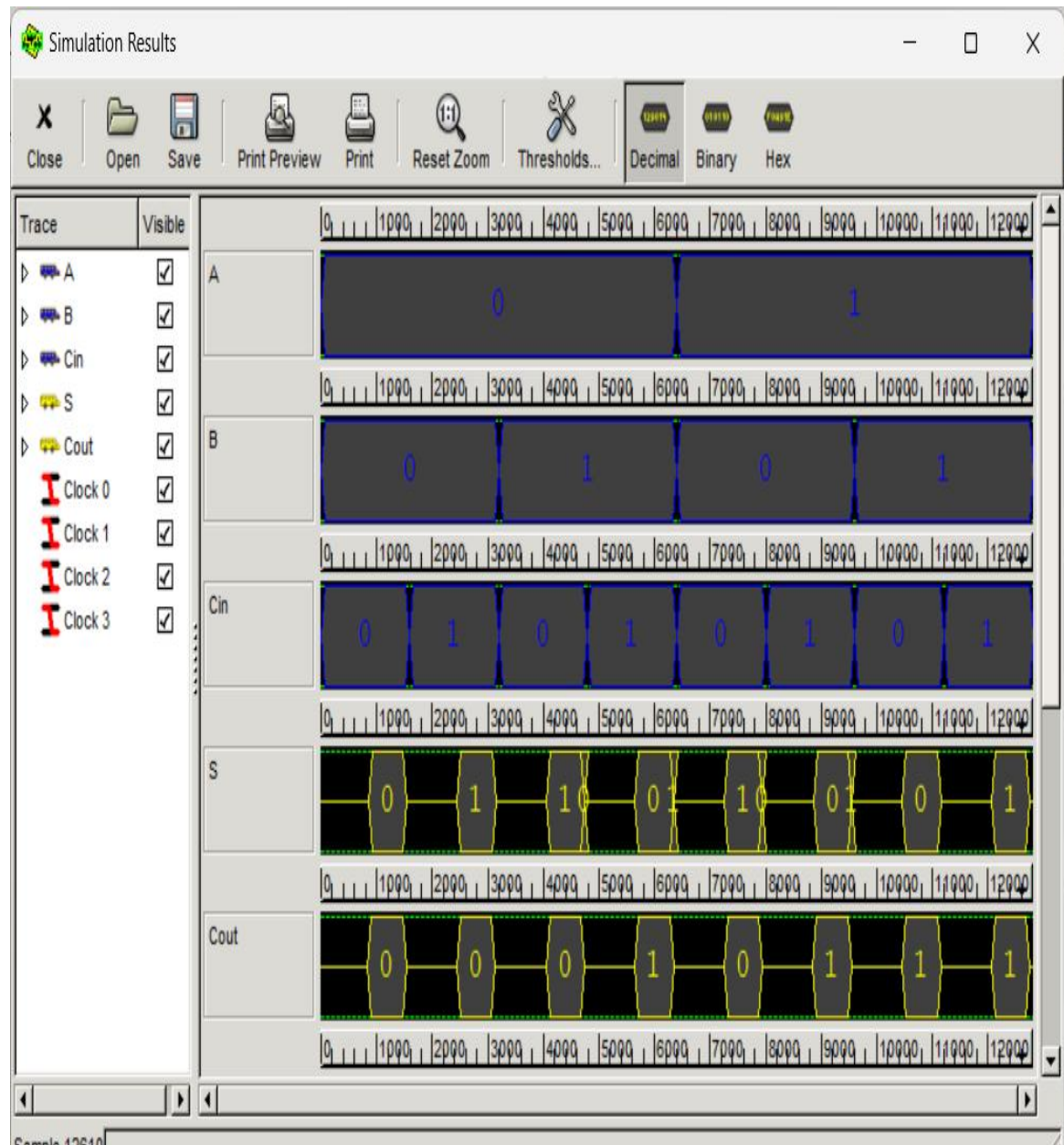
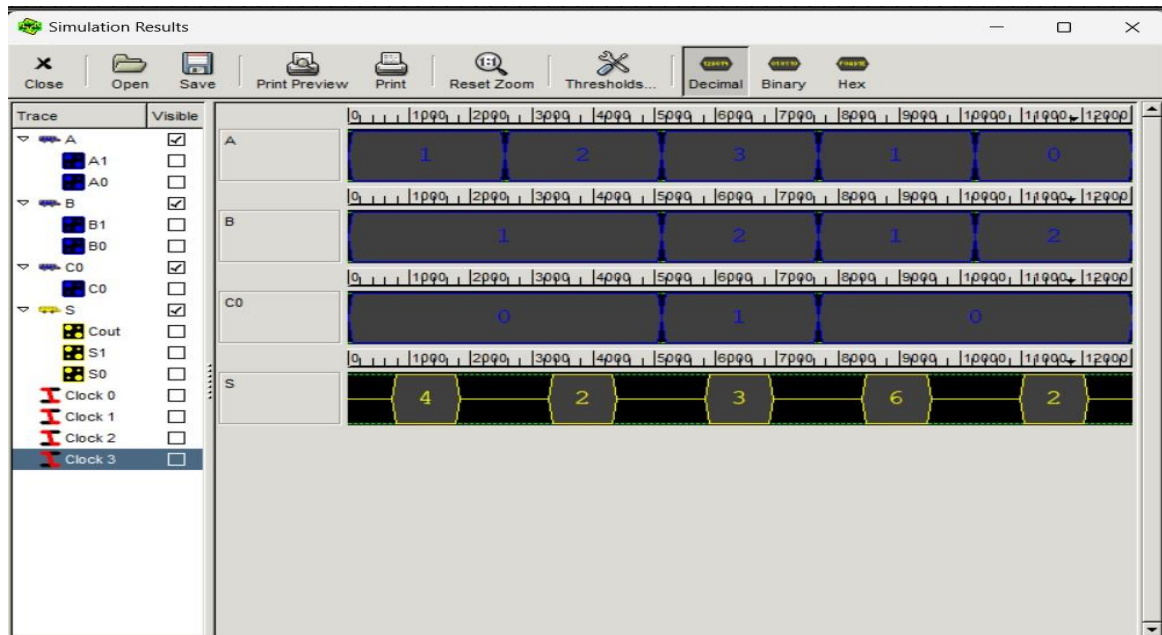


Fig 6.1.1: Full adder simulations using qca designer 2.0.3

This is the simulated waveforms result of the Full adder where we have given the input at the vector table in the binary format of 8bit then we can get the output sequence in the simulations results as required to the given inputs in the vector table.

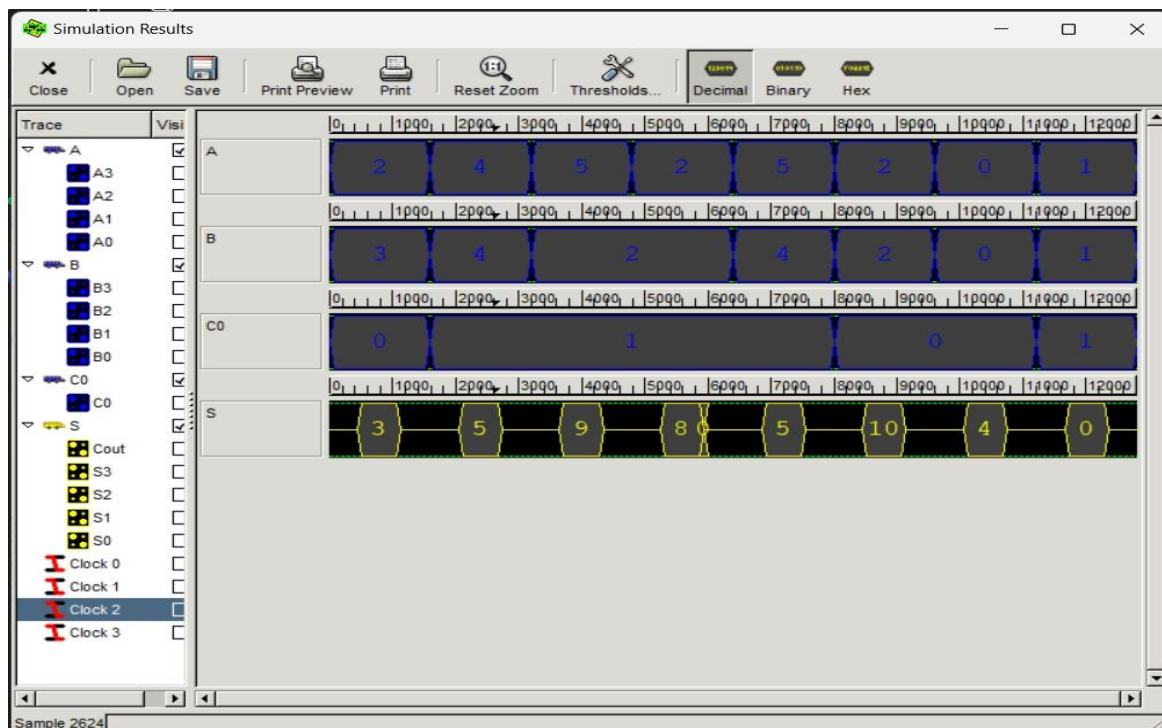
## 2. 2-BIT RCA



**Fig 6.1.2: 2-Bit rca simulations using qca designer 2.0.3**

This is the simulated waveforms of the 2-BIT RCA in this while creating the buses the same named bits are summed together and created as a single bus .In vector table we have given the inputs as binary format of 2 bits which is summed up and taken as 1 bit and got the output as required to the vector table.

## 3. 4-BIT RCA



**Fig 6.1.3: 4-Bit rca simulations using qca designer 2.0.3**

This is the simulated waveforms of the 4-BIT RCA In this while creating the buses

the same named bits are summed together and created as the single bus .In the vector table we have given input as binary format of 4 bits which is summed up and taken as 1 bit and get the result as required in the vector table.

## 4. 8-BIT RCA

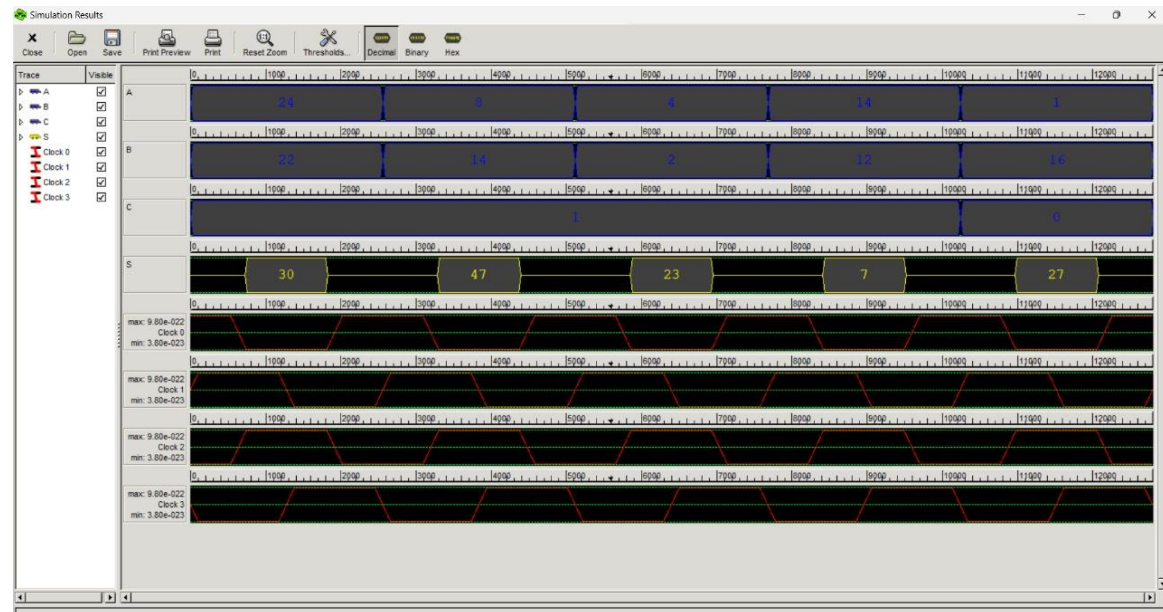


Fig 6.1.4: 8-Bit simulations using qca designer 2.0.3

This is the simulated waveforms of the 8-BIT RCA In this while creating the buses the same named buses are summed together and created a single bus. In the vector table we have given the input as binary format of 8 bits which is summed up and taken as a 1 bit and get the result as required in the vector table.

## 6.2 ENERGY DISSIPATION OF ADDERS

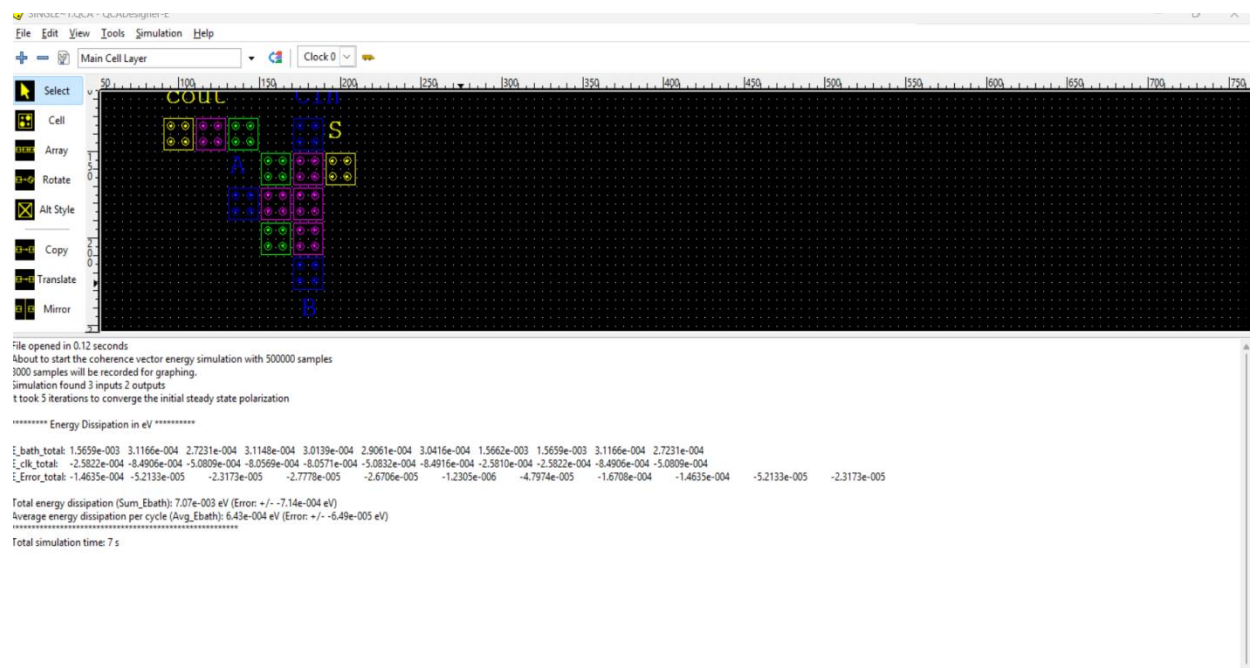
Energy dissipation is obtained by the software called QCA Designer E, where here the layout is placed in the software and start the simulation, after the simulation we get the Total and Average Energy Dissipation.

We get the simulations by opening the layout which is designed in the QCA Designer 2.0.3 and simulate it and gain the Energy and Average Energy Dissipation.

### 1. FULL ADDER

A full adder is a key digital circuit used in binary addition, capable of adding three binary digits: two significant bits and a carry input from a previous addition. It produces two outputs: the sum and the carry-out. The sum is calculated using the XOR operation, represented by the formula  $\text{Sum (S)} = A \oplus B \oplus \text{Cin}$ , while the

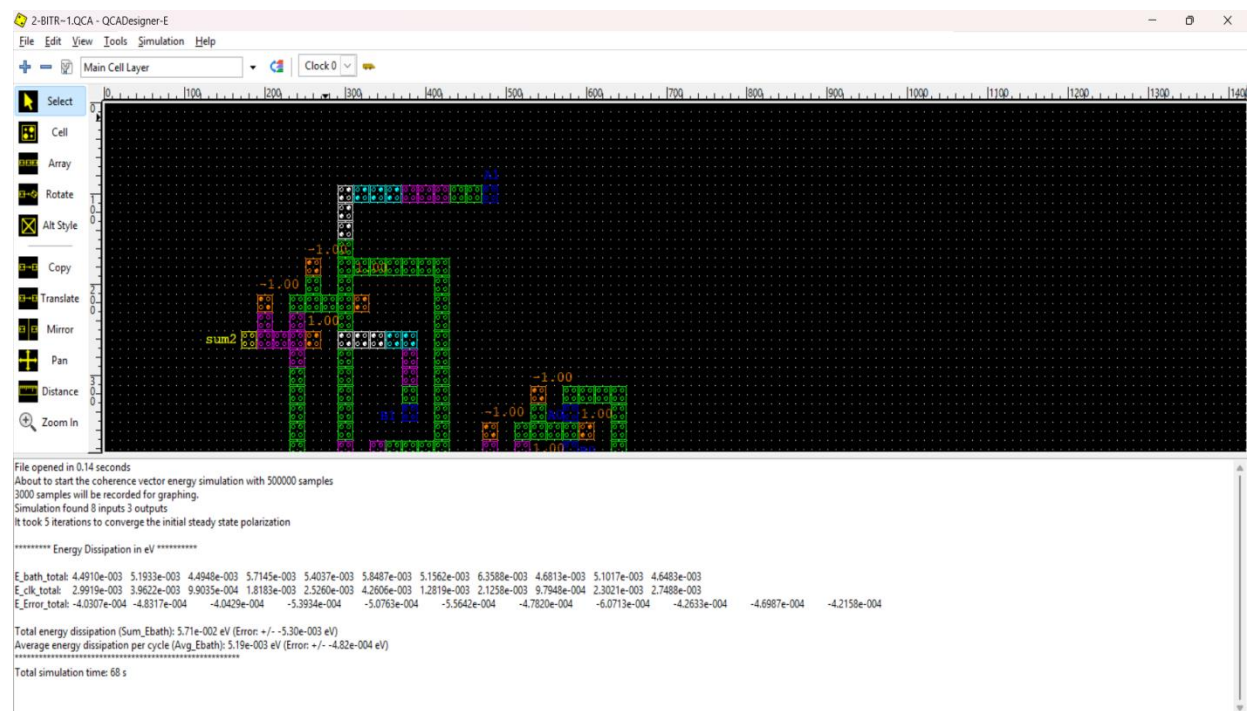
carry-out is determined by the combination of AND and OR operations, given by  
Carry-out ( $C_{out}$ ) =  $(A \text{ AND } B) \text{ OR } (C_{in} \text{ AND } (A \oplus B))$ .



**Fig 6.2.1: Energy analysis of full adder using qca designer e**

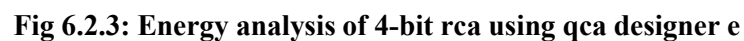
Total Energy Dissipation of the full adder is  $7.07 \times 10^{-3}$  ev and Average Energy Dissipation is  $6.43 \times 10^{-4}$  ev obtained by using the QCA Designer E.

## 2. 2-BIT RCA

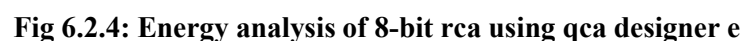


**Fig 6.2.2: Energy analysis of 2-bit rca using qca designer e**

### 3. 4-BIT RCA



## 4. 8-BIT RCA



Total Energy Dissipation of the full adder is  $1.39 \times 10^{-1}$  ev and Average Energy Dissipation is  $1.26 \times 10^{-2}$  ev obtained by using the QCA Designer E.

**Table 6.1 : Comparison of Energy Dissipation**

DESIGN	QCA IMPLEMENTATION		CMOS IMPLEMENTATION
	QCA CKT TOTAL ENERGY DISSIPATION IN ev	QCA CKT AVERAGE ENERGY DISSIPATION IN ev	CMOS CIRCUIT ENERGY DISSIPATION IN ev
FULL ADDER	$7.07 \times 10^{-3}$	$6.43 \times 10^{-4}$	$1.25 \times 10^{10}$
2-BIT RCA	$1.59 \times 10^2$	$1.44 \times 10^{-3}$	$6.24 \times 10^{-3}$
4-BIT RCA	$4.5 \times 10^{-2}$	$4.12 \times 10^{-3}$	$3.24 \times 10^4$
8-BIT RCA	$1.39 \times 10^{-1}$	$1.26 \times 10^{-2}$	$8.6 \times 10^{13}$

Comparison to conventional cmos the 8-BIT RCA is reduces to 98%.

## CHAPTER 7

### CONCLUSION AND FUTURE SCOPE

#### 7.1 CONCLUSION

In conclusion, the project on "An 8-Bit Ripple Carry Adder Using Quantum Dot Cellular Automata (QCA) for Nanocomputing Applications" presents a promising step toward advancing digital computing at the nanoscale. The use of Quantum Dot Cellular Automata as a computational paradigm offers several compelling advantages over traditional CMOS-based technologies, including significantly reduced power consumption, compact circuit size, and potential for high-speed operation. This project highlights the effectiveness of QCA in implementing a fundamental arithmetic operation—a ripple carry adder—within the context of nanocomputing.

The ripple carry adder, while being one of the simplest binary addition circuits, serves as a crucial component in various arithmetic and computational tasks. In the proposed design, an 8-bit ripple carry adder was implemented using QCA-based logic gates, which are constructed by arranging quantum cells in specific patterns to represent binary states. Unlike traditional semiconductor logic, QCA relies on the quantum interaction between dots to perform logical operations, removing the need for current flow and thus resulting in much lower power consumption. This characteristic of QCA makes it especially advantageous for applications where minimizing energy dissipation is critical, such as in portable devices, embedded systems, and future large-scale computing systems.

The design process begins with creating fundamental logic gates—AND, OR, XOR, and NOT—using quantum dots. These gates are then combined to form a full adder, which in turn is cascaded in a ripple carry configuration to create the 8-bit adder. While the ripple carry adder has the limitation of slower performance due to the sequential nature of carry propagation, its simplicity and ease of implementation made it an ideal candidate for demonstrating the capabilities of QCA in the realm of digital circuits. The circuit's functionality was tested through extensive simulation, and the results were analyzed to assess key performance metrics such as propagation delay, power consumption, and circuit area. These gates are then combined to form a full adder, which in turn is cascaded in a ripple carry configuration to create the 8-bit adder.

## 7.2 APPLICATIONS

### 1. Quantum Arithmetic Logic Units (ALUs)

An **Arithmetic Logic Unit (ALU)** is essential for any computational system, as it performs arithmetic and logic operations. Using QCA for an 8-bit RCA can enable the creation of efficient ALUs with high-speed operations, potentially leading to better performance than classical CMOS-based ALUs. The key advantage is the use of quantum properties like parallelism and entanglement to speed up operations.

### 2. Quantum Simulations

**Quantum simulations** of classical systems often require arithmetic operations like addition and multiplication. By implementing efficient **quantum arithmetic circuits** like an 8-bit RCA, researchers can use QCA to simulate complex quantum phenomena in a more compact and efficient way, accelerating the process of scientific simulations (e.g., quantum chemistry simulations, materials science, etc.).

### 3. Quantum Cryptography and Secure Communications

**Quantum cryptography** relies on quantum mechanical principles to achieve secure communication. Using QCA-based 8-bit RCAs can assist in the development of quantum cryptographic systems, especially in **quantum key generation** or **quantum encryption** algorithms. Arithmetic operations are vital in encryption schemes, and the use of quantum cellular automata may provide advantages in terms of speed and security.

### 4. Digital Signal Processing (DSP)

**Digital signal processing (DSP)** is crucial in communication systems, audio and image processing, and more. An 8-bit RCA designed using QCA could potentially be used in **quantum DSP systems**, where quantum processors handle signal filtering, compression, and transformations with greater efficiency than traditional systems.

### 5. Quantum Machine Learning

The development of quantum machine learning algorithms requires the implementation of classical computing tasks (like additions) in a quantum manner.

**8-bit RCAs** implemented in QCA could play a role in building faster arithmetic operations for machine learning models, improving the efficiency of quantum machine learning tasks and data processing. QML aims to leverage the unique properties of quantum systems, such as superposition, entanglement, and interference, to improve the performance and efficiency of machine learning models.

### 6. Quantum Control Systems

**Quantum control** is essential for the operation of quantum computers and quantum sensors. Using an 8-bit RCA in quantum cellular automata could help design **control circuits** that perform the necessary logic operations to manage the quantum state transitions, error correction, and other tasks in a quantum system.

## 7. Quantum Error Correction

Quantum error correction is crucial for ensuring that quantum information remains intact in the presence of noise. Arithmetic operations like addition and subtraction are integral to error correction algorithms. An 8-bit RCA in QCA could be utilized in **quantum error correction codes** to perform these operations at the quantum level, improving the stability of quantum computers. Arithmetic operations like addition and subtraction are integral to error correction algorithms.

## 8. Quantum Computing Hardware Design

As quantum computing hardware matures, there will be a need for efficient, scalable, and high-speed quantum circuits. Implementing an **8-bit RCA** using QCA in hardware design could help create compact and low-power components for quantum processors, paving the way for large-scale quantum computing systems.

## 9. Low Power Computation

**Quantum Cellular Automata** are inherently low-power due to their design, and implementing an 8-bit RCA in QCA could lead to the creation of low-power computing systems. This is especially important in fields like mobile computing and embedded systems, where energy efficiency is a critical factor. Additionally, QCA devices can operate at high speeds, typically in the range of gigahertz (GHz), making them suitable for high-performance computing applications. The scalability of QCA devices is another advantage, as they can be scaled down to very small sizes, reducing energy dissipation. This is especially important in fields like mobile computing and embedded systems.

## 10. Integration with Quantum Logic Gates

Quantum logic gates are the fundamental building blocks for quantum computations. Integrating an **8-bit RCA** into quantum circuits as part of a larger system of quantum gates could enable the development of quantum adders and other arithmetic logic operations as part of quantum algorithms.

## 7.3 ADVANTAGES

### 1. Low Power Consumption

**Quantum Cellular Automata (QCA)** operates at much lower power levels than traditional CMOS-based circuits. In QCA, the computation is based on the quantum state of the cells, which does not require continuous power supply like conventional transistors. This is especially important in energy-sensitive applications such as mobile devices, embedded systems, and large-scale quantum computing.

### 2. High-Speed Operation

**QCA-based circuits** can potentially operate at much higher speeds than classical CMOS circuits. This is because QCA can utilize **quantum parallelism** and exploit quantum mechanics principles to perform operations faster. For an **8-bit RCA**, QCA can reduce propagation delay, leading to faster computation and more efficient addition of binary numbers.

### 3. Reduced Area (Miniaturization)

**Quantum Cellular Automata** allows for the **miniaturization** of circuits. QCA-based designs are inherently smaller than traditional CMOS circuits due to the unique way information is stored and processed (using quantum states instead of physical transistors). This can lead to an increase in integration density, allowing more operations to be performed in a smaller space, which is important for building compact quantum processors.

### 4. Scalability

**QCA circuits** are highly scalable due to their small size and efficient design. The ability to scale the 8-bit RCA using QCA means that it could easily be expanded to larger systems, such as 16-bit or 32-bit RCAs, without significant increases in power or space requirements. This scalability makes QCA a promising candidate for large-scale quantum processors or digital systems. The ability to scale the 8-bit RCA using QCA means that it could easily be expanded to larger systems,

### 5. Reduced Delays (Faster Propagation)

QCA circuits can offer **faster signal propagation** due to the lack of charge-based current flow and slower transistor switching times seen in traditional CMOS technology. In an 8-bit RCA, this can reduce the delay that normally accumulates in the carry chain (which is a significant issue in classical RCAs), leading to quicker arithmetic operations.

### 6. No Current Flow

Unlike conventional circuits, **QCA does not rely on current flow** to process information. Instead, information is processed through the orientation of quantum cells (using electron charge configurations). This eliminates power dissipation caused by current leakage in traditional CMOS circuits, which is especially advantageous for high-performance applications.

## **7. Quantum Advantage for Parallelism**

**Quantum parallelism** allows multiple states to be processed simultaneously. While this may not directly translate to parallel processing in a classical sense, the use of quantum principles in QCA-based 8-bit RCA may result in the ability to perform multiple operations or simultaneous state transitions, accelerating arithmetic computations in quantum algorithms.

## **8. Fault Tolerance and Robustness**

**QCA can be designed with inherent fault tolerance.** While quantum systems are sensitive to noise, QCA circuits can be robust against some types of errors because they rely on the spatial configuration of cells rather than precise voltage or current signals. This makes the 8-bit RCA in QCA more resilient to errors compared to traditional circuits. rather than precise voltage or current signals. This makes the 8-bit RCA

## **9. Cost-Efficiency in Fabrication**

**Quantum Cellular Automata** uses a simpler physical model for computation, which may lead to more cost-effective fabrication in the long run. Although quantum computing technology is still developing, QCA-based circuits have the potential to be cheaper to fabricate at large scales compared to traditional transistor-based circuits.

## **10. Integration with Quantum Computing**

Since QCA inherently involves quantum principles, an **8-bit RCA** designed using QCA could be easily integrated into quantum computing systems. As quantum computers evolve, being able to use quantum-native components like QCA for arithmetic operations (such as in a quantum processor's arithmetic logic unit) could lead to better synergy between classical and quantum parts of a hybrid system.

## **11. Potential for Error Correction**

**Quantum error correction** is vital for quantum computing, and QCA circuits can be designed with inherent error resilience. The design of QCA-based 8-bit RCAs could incorporate error-correcting mechanisms at the circuit level, reducing the impact of quantum decoherence and noise that are common in quantum systems.

## **12. Higher Density of Logic Functions**

**QCA-based logic gates** can be made more compact and densely packed than their CMOS counterparts. For example, the size of an 8-bit RCA could be reduced in comparison to its traditional implementation, allowing more complex systems to fit into the same physical space. This is particularly valuable when designing systems like quantum processors that require high density of operations.

## **13. Future Proofing for Quantum Technologies**

While **quantum computing** and **QCA** are still in relatively early stages, they represent the future of high-performance computing. By designing quantum-native components such as an 8-bit RCA using QCA, engineers can create systems that are better equipped. This positions them to leverage the full potential of quantum hardware as it becomes more mainstream.

## **7.4 FUTURE SCOPE**

The future scope of 8-bit Ripple Carry Adder (RCA) using Quantum-dot Cellular Automata (QCA) is promising and exciting. QCA-based RCAs can potentially achieve higher speeds than traditional CMOS-based designs, making them suitable for high-performance computing applications. Additionally, QCA-based RCAs can consume significantly less power than traditional CMOS-based designs, making them suitable for energy-efficient computing applications.

The scalability of QCA-based RCAs is another significant advantage. They can be easily scaled up to larger bit widths, making them suitable for a wide range of applications, from embedded systems to high-performance computing. Furthermore, QCA-based RCAs can be integrated with other emerging technologies, such as memristor-based logic and spintronics, to create hybrid computing systems that offer improved performance, power efficiency, and scalability.

## REFERENCES

- [1] Pudi, V., Sridharan, K.: ‘Low complexity design of ripple carry and Brent-Kung adders in QCA’, IEEE Trans. Nanotechnol., 2012, 11, (1), pp. 105–119
- [2] M. Vahabi, A. N. Bahar, A. Otsuki and K. A. Wahid, "Ultra-low-cost design of ripple carry adder to design nanoelectronics in QCA nanotechnology," Electronics, vol. 11, no. 15, p. 2320, 2022.
- [3] S. Seyedi, B. Pourghebleh and N. Jafari Navimipour, "A new coplanar design of a 4-bit ripple carry adder based on quantum-dot cellular automata technology," ET Circuits, Devices & Systems, vol. 16, no. 1, pp. 64-70, 2022.
- [4] T.N. Sasamal et al. Efficient design of coplanar ripple carry adder in QCA IET Circuits Devices Syst, (2018).
- [5]“Efficient design of coplanar ripple carry adder in QCA”, Trailokya Nath Sasamal<sup>1</sup>, Ashutosh Kumar Singh<sup>2</sup>, Umesh Ghanekar<sup>1</sup>, 27th February 2018.
- [6] Sonars, N.: Design and Simulation Study of Coplanar Full Adder and Ripple Carry Adder Using Quantum Dot Cellular Automata. National Institute of Technology (2018)
- [7] Senthilnathan, S., Kumaravel, S.: Structural and power analysis of ripple carry adder in QCA. ARPN J. Eng. Appl. Sci. 13(8), (2006)
- [8] Balali, M., Rezai, A.: Design of low-complexity and high-speed coplanar four-bit ripple Carry adder in QCA technology. Int. J. Theor. Phys. 57(7), 1948–1960 (2018)

## **APPENDIX**

### **QCA DESIGNER E**

QCA Designer E is a software tool used for designing and simulating Quantum-dot Cellular Automata (QCA) circuits. QCA is a revolutionary technology that uses quantum dots to represent binary information, offering a potential replacement for traditional transistor-based computing. QCA Designer E provides a user-friendly interface for designing QCA circuits, allowing users to create, simulate, and analyze QCA designs.

QCA Designer E offers a range of features, including a graphical user interface for designing QCA circuits, a simulator for testing and verifying QCA designs, and a library of QCA components and modules. The software also includes tools for optimizing QCA designs, such as minimizing clock delay and reducing energy consumption. Additionally, QCA Designer E allows users to export QCA designs in various formats, including VHDL and Verilog, for further analysis and implementation.

QCA Designer E is widely used in research and development of QCA-based digital systems, including arithmetic circuits, logic circuits, and memory devices. The software is also used in educational institutions to teach QCA design and simulation techniques. Overall, QCA Designer E is a powerful tool for designing and simulating QCA circuits, enabling researchers and developers to explore the potential of QCA technology.